

# Neutrinos, Inflation & Higgs Vacuum Stability

Alexander Fraser Spencer-Smith

SUSY 2013

August 30, 2013

Archil Kobakhidze & A.F.S-S [1301.2846] & [1305.7283]



THE UNIVERSITY OF  
**SYDNEY**

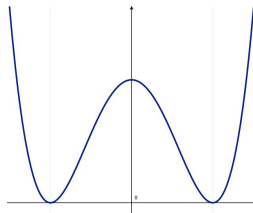


**CoEPP**  
ARC Centre of Excellence for  
Particle Physics at the Terascale

- ATLAS & CMS announced the discovery of a new boson with mass  $\approx 125 - 126$  GeV.
- Further measurements have shown that it's a Higgs boson, perhaps even *the* Higgs boson.
- Let's assume it's *the*!
- What are the implications for new physics?

- Classical SM Higgs potential in unitary gauge

$$V(h) = \frac{\lambda}{4} \left( h^2 - v_{EW}^2 \right)^2 \quad (1)$$



- RG improved effective potential for  $h$

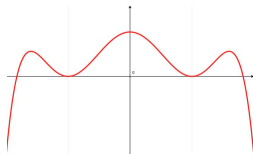
$$V_{eff}^{(1-loop)}(h) = \frac{\lambda(h)}{4} \left( h^2 - v_{EW}^2 \right), \quad (2)$$

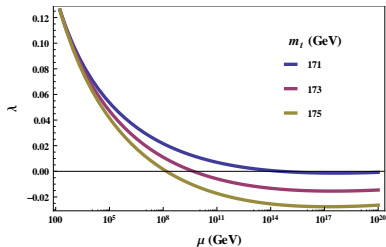
$$\lambda(h) = \lambda(\mu) + \beta_\lambda \ln \left[ \frac{h}{\mu} \right], \quad (3)$$

$$(4\pi)^2 \beta_\lambda \approx 24\lambda^2 - 6y_t^4 + \dots, \quad (4)$$

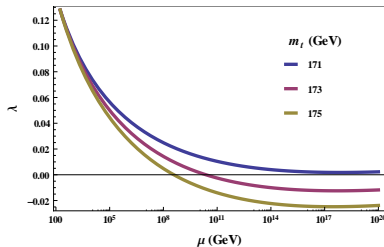
$$y_t(m_t) \approx 1 \ \& \ \lambda(m_t) \approx 0.12 \quad (5)$$

$$\Rightarrow \beta_\lambda(m_t) < 0. \quad (6)$$





(a)  $m_h = 125$  GeV



(b)  $m_h = 126$  GeV

- $\lambda(\mu_I) = 0$  for  $\mu_I \approx 10^{10}$  GeV.

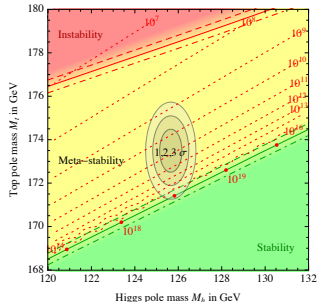
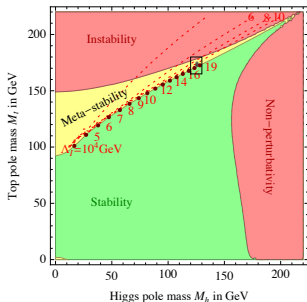
# Flat-spacetime Estimate of Decay Probability

- EW vacuum can decay to true vacuum.
- Using Coleman's prescription obtain decay probability using instanton/bounce solution to Euclidean EOM for  $h$  in  $V(h)$ ,

$$p \approx e^{-B}, \quad (7)$$

$$B_{LW} = \frac{8\pi^2}{3|\lambda(\mu_m)|} \quad (8)$$

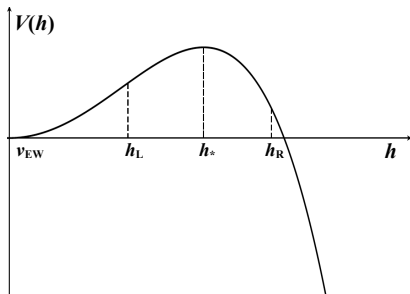
- SM EW vacuum in flat spacetime is *metastable*.



(Buttazzo et. al. [hep-ph:1307.3536])

# Vacuum Stability During Inflation

- Taking into account cosmological history of the universe we must examine the decay rate of  $v_{EW}$  during inflation.
- In a cosmological spacetime  $v_{EW}$  can also decay via
  - Thermal activation
  - Production of large amplitude Higgs perturbations during inflation (Espinosa et. al. [hep-ph:0710.2484])
  - Instantons (Hawking-Moss or Coleman-deLuccia) (Archil Kobakhidze & A.F.S-S [hep-ph:1301.2846])



- Instantons dominate, type is model dependent:

- Negligible inflaton-Higgs interactions: HM instanton dominates

$$B_{HM} = \frac{8\pi^2}{3} \frac{\lambda(\mu_I e^{-1/4})\mu_I^4 e}{4H_{inf}^4} \quad (9)$$

- Sizable inflaton-Higgs interactions (fine tuning needed): CdL instanton dominates. In this case the rate of decay is exponentially enhanced and inflation ceases globally.

$$B_{CdL} = -\frac{2\pi^2}{\lambda} I, \quad (10)$$

where

$$I = \int_0^\infty x^3 dx \left[ h^2(x) \left( 1 - \frac{h^2(x)}{2h_*^2} \right) \right] < 0. \quad (11)$$

with

$$h(x) = \begin{cases} 8h_R \left( 8 + \left( \frac{h_R}{h_*} \right)^2 x^2 \right)^{-1}, & 0 \leq x < x_* \\ \frac{x_* h_*}{x(J_1(ix_*) + iY_1(-ix_*))} (J_1(ix) + iY_1(-ix)), & x_* < x < \infty \end{cases}, \quad (12)$$

$$x_* = \frac{2\sqrt{2}h_*}{h_R} \left( \frac{h_R}{h_*} - 1 \right)^{1/2}. \quad (13)$$

- Requiring that decay processes do not prevent inflation from proceeding globally we obtain, for models with negligible inflaton-Higgs interactions, the bound

$$H_{inf} < 1.7 \times 10^9 (1 \times 10^{12}) \text{ GeV} \quad (14)$$

for  $m_h = 126 \text{ GeV}$ ,  $m_t = 174(172) \text{ GeV}$ .

- Relating the bound to CMB observables we find:
  - $\eta < 0$ : Only small field models are viable/large field models ruled out
  - $r \approx 10^{-11}(10^{-5})$ : The ratio of tensor to scalar perturbations in the CMB must be tiny - if Planck sees tensor perturbations then all models of inflation are ruled out, unless there is new physics beyond the SM, responsible for stabilisation of the EW vacuum.
- Argument also applies to curvaton models.



- Stability of EW vacuum depends on whether  $\lambda$  runs negative or not  $\Rightarrow$  New physics before  $\mu_I \approx 10^{10}$  GeV.
- Typically one works in  $\overline{MS}$  and any effect on couplings arises as
  - Modification of  $\beta$ -functions
  - Threshold corrections to effective couplingsat heavy particle thresholds/symmetry breaking VEVs
- Three ways to implement an extension to the SM, affecting running of  $\lambda$ :
  - Affect  $\lambda$  directly (scalars)
  - Affect the largest Yukawa couplings (fermions)
  - Embed the EW gauge group into a larger group to affect the gauge couplings (gauge groups)

- Established evidence for physics beyond the SM: Neutrino masses, Dark Matter & Dark Energy
- What can vacuum stability tell us about Neutrino masses?
- Type-I & III seesaws, add fermions, stability condition:  $\lambda > 0$
- Type-I seesaw mechanism, add  $\nu_R$  to the SM
- 'Typical' seesaw with  $M_R \approx 10^{15}$  GeV automatically ruled out
- Need  $M_R < \mu_I$  (low scale seesaw)
  - For large  $\sigma$  new Yukawa couplings acts like top  $\Rightarrow \lambda$  runs negative quicker!  
 $\Rightarrow$  unstable EW vacuum (Rodejohann, Zhang [hep-ph:1203.3825])
  - For smaller  $\sigma$  find  $3.3 \text{ TeV} < M_R < 4.5 \text{ TeV}$  from LFV and  $(0\nu\beta\beta)$   
(Chakraborty et. al. [hep-ph:1207.2027])
- Type-III seesaw mechanism (triplet fermions) argument is similar with relaxed bounds for case of smaller  $\sigma$ .

- Extend scalar sector with EW triplet of scalars

$$\begin{aligned}
 V(\phi, \Delta) = & -m_\phi^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2 + m_\Delta^2 \text{tr}(\Delta^\dagger \Delta) + \frac{\lambda_1}{2} (\text{tr}(\Delta^\dagger \Delta))^2 \\
 & + \frac{\lambda_2}{2} \left[ (\text{tr}(\Delta^\dagger \Delta))^2 - \text{tr}(\Delta^\dagger \Delta)^2 \right] + \lambda_4 (\phi^\dagger \phi) \text{tr}(\Delta^\dagger \Delta) \\
 & + \lambda_5 \phi^\dagger [\Delta^\dagger, \Delta] \phi + \left[ \frac{\lambda_6}{\sqrt{2}} \phi^T i \sigma_2 \Delta^\dagger \phi + \text{h.c.} \right]. \quad (15)
 \end{aligned}$$

- All except  $\lambda, m_\phi$  are arbitrary, just need to make sure we can avoid instability and triviality from choice of boundary conditions at  $m_\Delta$
- Many stability conditions (Ahrif et. al. [hep-ph:1105.1925]):

$$\lambda > 0, \quad (16)$$

$$\lambda_1 > 0, \quad (17)$$

$$\lambda_1 + \frac{\lambda_2}{2} > 0, \quad (18)$$

$$\lambda_4 \pm \lambda_5 + 2\sqrt{\lambda\lambda_1} > 0, \quad (19)$$

$$\lambda_4 \pm \lambda_5 + 2\sqrt{\lambda \left( \lambda_1 + \frac{\lambda_2}{2} \right)} > 0. \quad (20)$$

- Threshold correction:

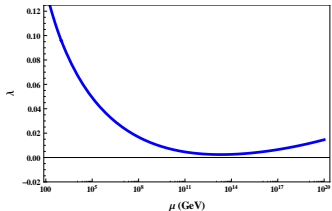
$$\lambda_h = \lambda - \frac{\lambda_6^2}{2m_\Delta^2}. \quad (21)$$

- Modification of  $\beta_\lambda$

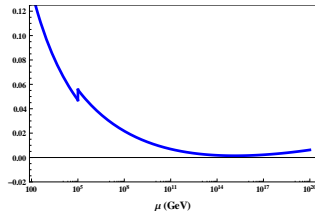
$$\begin{aligned} \beta_{\lambda_h}^{(1)} = \lambda_h \left( -9g_2^2 - 3g_1^2 + 12y_t^2 \right) + 24\lambda_h^2 + \frac{3}{4}g_2^4 \\ + \frac{3}{8} \left( g_1^2 + g_2^2 \right)^2 - 6y_t^4 \end{aligned} \quad (22)$$

$$\begin{aligned} \rightarrow \beta_\lambda^{(1)} = \lambda \left( -9g_2^2 - 3g_1^2 + 12y_t^2 \right) + 24\lambda^2 + \frac{3}{4}g_2^4 \\ + \frac{3}{8} \left( g_1^2 + g_2^2 \right)^2 - 6y_t^4 + 3\lambda_4^2 + 2\lambda_5^2 \end{aligned} \quad (23)$$

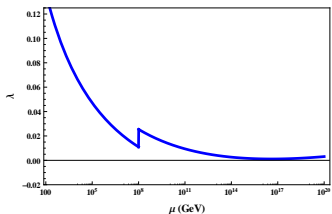
# Vacuum Stability in a Type-II Seesaw Model



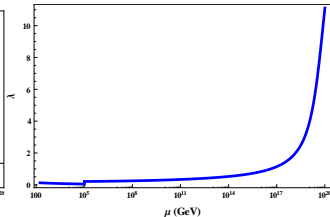
(c)  $m_{\Delta} = 1 \text{ TeV}$ .



(d)  $m_{\Delta} = 100 \text{ TeV}$ .



(e)  $m_{\Delta} = 10^8 \text{ GeV}$ .



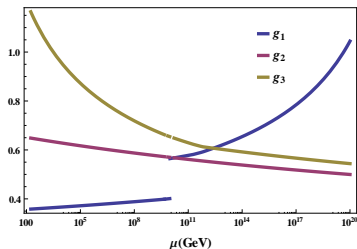
(f)  $m_{\Delta} = 100 \text{ TeV}$ .

Figure: One loop running of  $\lambda$  in the type-II seesaw model, with  $m_h = 125 \text{ GeV}$  and  $m_t = 173 \text{ GeV}$ . (Archil Kobakhidze & A.F.S-S [hep-ph:1305.7283])

- What about gauge, Yukawa *and* scalar sector effects?
- LR Symmetric model:  $SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$
- Minimal scalar content:  $\phi_L \in (\mathbf{1}, \mathbf{1}, \mathbf{2}, 1/2)$ ,  $\phi_R \in (\mathbf{1}, \mathbf{2}, \mathbf{1}, 1/2)$ , need vectorlike fermion  $F_i$  for each SM fermion (ALRSM (Davidson & Wali, PRL '87)).
- Scalar potential

$$V(\phi_L, \phi_R) = -m^2 \left( \phi_L^\dagger \phi_L + \phi_R^\dagger \phi_R \right) + \frac{\lambda}{2} \left( \phi_L^\dagger \phi_L + \phi_R^\dagger \phi_R \right)^2 + \sigma \phi_L^\dagger \phi_L \phi_R^\dagger \phi_R. \quad (24)$$

- Bounded from below for  $\lambda > 0$  and  $\sigma > -2\lambda$
- Two vacua, parity breaking for  $\sigma > 0$  with  $|v_R|^2 = \frac{m^2}{\lambda}$  and  $v_L = 0$
- Hierarchy of scalar masses for  $\sigma \ll \lambda$ .
- Note:  $v_L \neq 0$  radiatively and theory can be consistently matched to the SM EFT at one loop (Archil Kobakhidze & A.F.S-S [hep-ph:1305.7283])

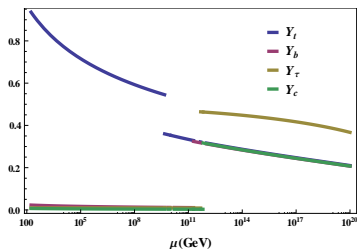


(a) Running gauge couplings with  $M_T = 4.7 \times 10^9$  GeV and  $m = 1 \times 10^{10}$  GeV.

- $g_1$  matched at  $v_R$  as

$$g_1 = \frac{g_R g_{B-L}}{\sqrt{g_R^2 + g_{B-L}^2}} = \frac{g_2 g_{B-L}}{\sqrt{g_2^2 + g_{B-L}^2}}, \quad (25)$$

- Vector-like fermions in a hierarchy to prevent a Landau pole for  $g_1$ .



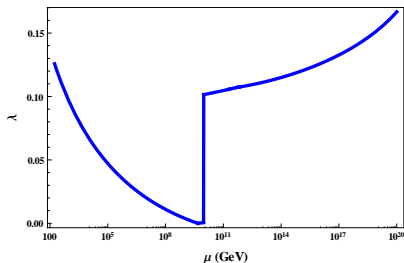
(b) Running Yukawa couplings.

- $y_{F_i}$  matched at  $M_{F_i}$  with

$$y_{f_i} = y_{F_i}^2 \frac{v_R}{M_{F_i}}. \quad (26)$$

- Yukawas all become  $\mathcal{O}(y_T)$  (universal seesaw).





(c) Running Higgs quartic coupling

**Figure:** Running couplings in the ALRSM with  $M_T = 4.7 \times 10^9$  GeV and  $m = 1 \times 10^{10}$  GeV.

- $\lambda$  matched at  $m_R$  with

$$\frac{\lambda_{eff}}{8} = \frac{3y^4}{16\pi^2} \left( \frac{1}{4} - \frac{5}{8} \ln \left[ \frac{M_T^2 + \frac{m^2 y_T^2}{\lambda}}{m_R^2} \right] \right) - \frac{9\lambda^2}{256\pi^2}, \quad (27)$$

- $\lambda > 0$  can be satisfied, for  $m_R \approx \mu_I$ .

- Flat space-time analysis of Higgs vacuum stability shows EW vacuum is *metastable*
- Curved space-time analysis shows the EW vacuum is *unstable* unless the rate of inflation is low enough
- Possible Planck observation of tensor perturbations would provide a very strong hint of physics BSM
- Wide range of parameter space for (pure) type-I & type-III seesaw mechanisms excluded by consideration of EW vacuum stability
- Large range of parameter space possible for type-II seesaw
- ALRSM consistent with EW vacuum stability, demonstrates effects coming from gauge, Yukawa and scalar sectors
- Outside main line of talk, but ALRSM also exhibits some nice features:
  - Coleman-Weinberg mechanism generates VEV for Higgs radiatively
  - Universal seesaw mechanism generates Yukawa hierarchy