

Do we have the explanation for the families and their properties, for the scalar Higgs and Yukawa couplings and for the gauge vector fields?

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More than **30 years ago** the **standard model** offered an elegant new step in understanding the origin of fermions and bosons.

It postulated, stimulated by the observations:

- The existence of the **massless family members**;
coloured quarks and colourless leptons,
the **left handed members** distinguishing from the **right handed ones** in the **weak** and **hyper charges**.
- The existence of **families**.

α name	hand- edness $-4iS^{03}S^{12}$	weak charge τ^{13}	hyper charge Y	colour charge	elm charge Q
u_L^i	-1	$\frac{1}{2}$	$\frac{1}{6}$	colour triplet	$\frac{2}{3}$
d_L^i	-1	$-\frac{1}{2}$	$\frac{1}{6}$	colour triplet	$-\frac{1}{3}$
ν_L^i	-1	$\frac{1}{2}$	$-\frac{1}{2}$	colourless	0
e_L^i	-1	$-\frac{1}{2}$	$-\frac{1}{2}$	colourless	-1
u_R^i	1	weakless	$\frac{2}{3}$	colour triplet	$\frac{2}{3}$
d_R^i	1	weakless	$-\frac{1}{3}$	colour triplet	$-\frac{1}{3}$
ν_R^i	1	weakless	0	colourless	0
e_R^i	1	weakless	-1	colourless	-1

Members of each of the $i = 1, 2, 3$ massless families before the electroweak break.

And the **anti-fermions** to each family and family member.

- Three **massless vector fields**, the gauge fields to the observed **charges** of the family **members**, before the **electroweak break**.

name	hand- edness	weak charge	hyper charge	colour charge	elm charge
hyper photon	0	0	0	colourless	0
weak bosons	0	triplet	0	colourless	triplet
gluons	0	0	0	colour octet	0

They all are vectors in $d = (1 + 3)$, in the adjoint representations with respect to the weak, colour and hyper charges.

Elm. charge = weak charge + hyper charge.

- The existence of one **scalar field**, the **Higgs** (and the **anti Higgs**),
chosen to be a **weak doublet**, (like **fermions**) with the appropriate hyper charge in order to "dress" **right handed family members** with the weak and the hyper charge of their **left handed partners**
and to assure the appropriate mass ratios of **weak bosons**.
- **The existence** of the **Yukawa couplings**,

$$Y^\alpha \frac{v}{\sqrt{2}}$$

taking care of the masses of **fermions**, together with the **Higgs**.

- The Higgs field, the scalar in $d = (1 + 3)$, with $P_R = (-1)^{2s+3B+L} = 1$.

name	hand- edness	weak charge	hyper charge	colour charge	elm charge
0· Higgs _u	0	$\frac{1}{2}$	$\frac{1}{2}$	colourless	1
$\langle \text{Higgs}_d \rangle$	0	$-\frac{1}{2}$	$\frac{1}{2}$	colourless	0

name	hand- edness	weak charge	hyper charge	colour charge	elm charge
$\langle \text{Higgs}_u \rangle$	0	$\frac{1}{2}$	$-\frac{1}{2}$	colourless	0
0· Higgs _d	0	$-\frac{1}{2}$	$-\frac{1}{2}$	colourless	-1

Let us summarize the standard model assumptions

- All fermions have all the charges, which are not singlets, in the fundamental representations of the charge groups.
- All gauge bosons have all the charges, which are not singlets, in the adjoint representations of the corresponding groups. The singlet values are all zero for all the gauge fields.
- Higgs scalars are doublets with respect to the weak charge.
- Yukawa couplings carry the family quantum numbers.

The *standard model* assumptions have been confirmed without offering surprises.

The last unobserved field, the **scalar Higgs, detected in June 2012, was confirmed in March 2013.**

What questions should one urgently ask so that the answers would help to make the right next step beyond the standard model?

- **Why there exist families at all? Or rather: What is the origin of families?**
How many families are there? And what are their properties if there are more than the so far observed ones?
- **Why family members – quarks and leptons – manifest so different properties if they all start as massless?**



- How is the **origin of the scalar field** (the Higgs) and the **Yukawa couplings connected with the origin of families?** **How many scalar fields** determine properties of the so far (and others possibly to be) observed fermions and masses of bosons?
- **Why are all the scalar fields doublets with respect to the weak charge?** What are their **representations with respect to the family quantum numbers?**
- Where does the **dark matter originate?**
- Where do the **charges and correspondingly the so far (and others possibly be) observed gauge fields originate?**
- What is the dimension of the space? $(1 + 3)?$, $(1 + (d - 1))?$
What is d ?

- **What** is the role of the **symmetries**: discrete, continues, global and gauge, fermion-antifermion asymmetry?
- And many others.

My statement:

- **Next trustable step beyond the standard model must offer answers to several open questions not only to one.**
- **There exist not yet observed families, gauge fields, scalar fields.**
The appearance of Yukawa couplings speaks for several scalar fields.
- **Dimension of the space is large than 4.**



In the literature **NO explanation for the existence of the families can be found**. Several extensions of the **standard model** are, however, proposed, like:

- **A tiny** extension: The inclusion of the right handed neutrinos into the family.
- The $SU(3)$ group is assumed to describe – not explain – the existence of three families.
- Like Higgs has the charge in the fundamental representation of the group, also Yukawas are assumed to be scalar fields, in the bi-fundamental representation of the $SU(3)$ group.
- Supersymmetric theories assuming the existence of partners to the existing fermions and bosons, with charges in the opposite representations.

**The spin-charge-family-theory does offer
a possible explanation for the existence of families,
offering answers besides to the "urgent" open questions
also to many of the "not so urgent" open
questions, presented above.**

Content of the talk

- A brief introduction into the **spin-charge-family-theory**.
- Achievements of the **spin-charge-family-theory** so far.
- Some new predictions for the measurements.
- **Problems in this theory to be solved.**



The **Spin-Charge-Family-Theory** is offering **the explanation for:**

- The **existence of families and family members**.
- The **origin of several scalar fields**, which offer the (hopefully right) explanation for the **origin of mass matrices of fermions, correspondingly for the origin of Yukawa couplings and masses of gauge fields**.
- The **origin of charges**.
- The **origin of gauge fields**.
- The **origin of dark matter**.
- **And...**



Is the spin-charge-family theory the right way at least as a first step beyond the standard model?

- **Spinors** carry in $d \geq (1 + 13)$ **two kinds of the spin**. No charges.
In $d = (1 + 3)$ the **Dirac spin** (γ^a) takes care of **the spin and the charges of quarks and leptons**.
The **second kind of the spin** ($\tilde{\gamma}^a$) **generates families**.
- **Spinors** couple correspondingly to **vielbeins** and to two kinds of **spin connection fields**.
In $d = (1 + 3)$ the **spin-connection fields** together with the **vielbeins** manifest as the **gauge vector fields** and the **scalar fields**. The vacuum expectation values of the **scalar fields** determine masses of **fermions** on the tree level.

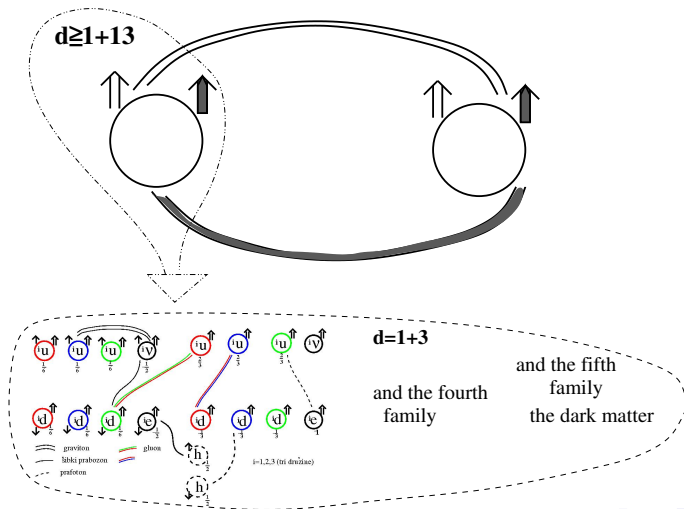
- A simple action in $d = (1 + 13)$ for **spinors** and **spin connections and vielbeins** manifests in $d = (1 + 3)$, after appropriate breaks of the starting symmetry, the **standard model action**
 - 1 for **fermions** – predicting the fourth **family** coupled to the so far observed three and the **dark matter family**,
 - 2 for **gauge fields**, predicting new ones,
 - 3 for **scalar fields**, which take care of **mass matrices** of **fermions** and **masses of weak bosons**, predicting several ones.



- All **vector boson fields** have all the **charges** in the **adjoint representations**.
- The **scalar fields** have the **family charges** in the **adjoint representations**, while they are **doublets** with respect to the **weak charge**.
- All **family members of all families** have all the charges in the **fundamental representations of the corresponding groups**.
- **No supersymmetry is predicted** at low energy regime.



Introduction



There are two kinds of the Clifford algebra objects (only two):

- The **Dirac γ^a operators** (used by Dirac 80 years ago).
- The **second one: $\tilde{\gamma}^a$** , which I recognized.

$$\{\gamma^a, \gamma^b\}_+ = 2\eta^{ab} = \{\tilde{\gamma}^a, \tilde{\gamma}^b\}_+,$$

$$\{\gamma^a, \tilde{\gamma}^b\}_+ = 0,$$

$$(\tilde{\gamma}^a \mathbf{B} : = \mathbf{i}(-)^{n_B} \mathbf{B} \gamma^a) |\psi_0 \rangle,$$

$$(\mathbf{B} = a_0 + a_a \gamma^a + a_{ab} \gamma^a \gamma^b + \dots + a_{a_1 \dots a_d} \gamma^{a_1} \dots \gamma^{a_d}) |\psi_0 \rangle$$

$(-)^{n_B} = +1, -1$, when the object B has a Clifford even or odd character, respectively.

$|\psi_0 \rangle$ is a vacuum state on which the operators γ^a apply.

$$\mathbf{S}^{ab} := (\mathbf{i}/4)(\gamma^a \gamma^b - \gamma^b \gamma^a),$$

$$\tilde{\mathbf{S}}^{ab} := (\mathbf{i}/4)(\tilde{\gamma}^a \tilde{\gamma}^b - \tilde{\gamma}^b \tilde{\gamma}^a),$$

$$\{\mathbf{S}^{ab}, \tilde{\mathbf{S}}^{cd}\}_- = \mathbf{0}.$$

- $\tilde{\mathbf{S}}^{ab}$ define the equivalent representations with respect to \mathbf{S}^{ab} .

My recognition:

- If γ^a are used to describe **the spin and the charges of spinors**,
 $\tilde{\gamma}^a$ can be used to describe families of spinors..

Must be used!!

A simple action for a **spinor** which carries in $d = (1 + 13)$ only **two kinds of a spin** (no charges) and for **the gauge fields**

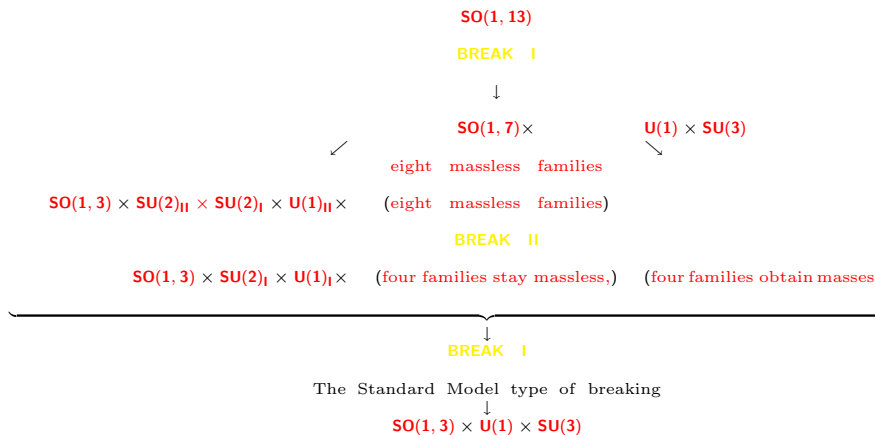
$$\mathbf{S} = \int d^d x E \mathcal{L}_f + \int d^d x E (\alpha R + \tilde{\alpha} \tilde{R})$$

$$\mathcal{L}_f = \frac{1}{2} (E \bar{\psi} \gamma^a p_{0a} \psi) + h.c.$$

$$p_{0a} = f^\alpha{}_a p_{0\alpha} + \frac{1}{2E} \{p_\alpha, E f^\alpha{}_a\} -$$

$$\mathbf{p}_{0\alpha} = \mathbf{p}_\alpha - \frac{1}{2} \mathbf{S}^{ab} \omega_{ab\alpha} - \frac{1}{2} \tilde{\mathbf{S}}^{ab} \tilde{\omega}_{ab\alpha}$$

- The only internal degrees of freedom of **spinors** (fermions) are the **two kinds of the spin**.
- The only **gauge fields** are the **gravitational ones** – **vielbeins and two kinds of spin connections**.

Breaks of symmetries when starting with **massless spinors**



- The action for spinors at the low energy regime

$$\mathcal{L}_f = \bar{\psi} \gamma^m (p_m - \sum_{A,i} g^A \tau^{Ai} A_m^{Ai}) \psi +$$

$$\left\{ \sum_{s=[7],[8]} \bar{\psi} \gamma^s p_{0s} \psi \right\} +$$

the rest ,

$$p_{0m} = f_m^\mu (p_\mu - \sum_A g^A \vec{\tau}^A \vec{A}_\mu^A),$$

$$p_{0s} = f_s^\sigma (p_\sigma - \sum_B g^B \vec{\tau}^B \vec{A}_\sigma^B - \sum_B \tilde{g}^B \vec{\tau}^B \vec{\tilde{A}}_\sigma^B).$$

$$\tau^{Ai} = \sum_{a,b} c^{Ai}_{ab} S^{ab}, \quad \tilde{\tau}^{Ai} = \sum_{a,b} \tilde{c}^{Ai}_{ab} \tilde{S}^{ab},$$

Before the last two breaks, BREAK II and Break I, of symmetries there are eight massless families of fermions.

- It is the term $\bar{\psi} \gamma^s p_{0s} \psi$, $s \in \{[7], [8]\}$ which determines mass of fermions on the tree level.
- Before the electroweak break (BREAK I) the four out of eight families remain massless. Four of the eight gain masses.
- The lowest among the **decoupled** upper, massive after the $SU(2)_{II} \times U(1)_{II}$ break, four families is the **candidate** for forming the **dark matter** clusters.



Our technique to represent spinors works elegantly.

- *J. of Math. Phys.* **43**, 5782-5803 (2002), hep-th/0111257,
- *J. of Math. Phys.* **44** 4817-4827 (2003), hep-th/0303224,
both with H.B. Nielsen.

$$\begin{matrix} \text{ab} \\ (\pm \mathbf{i}) \end{matrix} : = \frac{1}{2}(\gamma^{\mathbf{a}} \mp \gamma^{\mathbf{b}}), \quad \begin{matrix} \text{ab} \\ [\pm \mathbf{i}] \end{matrix} := \frac{1}{2}(1 \pm \gamma^{\mathbf{a}}\gamma^{\mathbf{b}})$$

$$\text{for } \eta^{aa}\eta^{bb} = -1,$$

$$\begin{matrix} \text{ab} \\ (\pm) \end{matrix} : = \frac{1}{2}(\gamma^{\mathbf{a}} \pm \mathbf{i}\gamma^{\mathbf{b}}), \quad \begin{matrix} \text{ab} \\ [\pm] \end{matrix} := \frac{1}{2}(1 \pm i\gamma^{\mathbf{a}}\gamma^{\mathbf{b}}),$$

$$\text{for } \eta^{aa}\eta^{bb} = 1$$

with $\gamma^{\mathbf{a}}$ which are the usual **Dirac operators**





$$\begin{aligned} \mathbf{S}^{ab}(\mathbf{k}) &= \frac{k^{ab}}{2}(\mathbf{k}), & \mathbf{S}^{ab}[\mathbf{k}] &= \frac{k^{ab}}{2}[\mathbf{k}], \\ \tilde{\mathbf{S}}^{ab}(\mathbf{k}) &= \frac{k^{ab}}{2}(\mathbf{k}), & \tilde{\mathbf{S}}^{ab}[\mathbf{k}] &= -\frac{k^{ab}}{2}[\mathbf{k}]. \end{aligned}$$



γ^a transforms $\binom{ab}{k}$ into $[-k]$, never to $\binom{ab}{k}$.

$\tilde{\gamma}^a$ transforms $\binom{ab}{k}$ into $\binom{ab}{k}$, never to $[-k]$.

S^{ab} generate **all the members of one family**. The eightplet (the representation of $SO(1, 7)$) of quarks of a particular colour charge

i		$ \psi_i\rangle$	$\Gamma^{(1,3)}$	S^{12}	$\Gamma^{(4)}$	τ^{13}	τ^{23}	Y	τ^4
		Octet, $\Gamma^{(1,7)} = 1$, $\Gamma^{(6)} = -1$, of quarks							
1	u_R^c1	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)(+) & & (+)(+) & & (+)(-) & (-) & (-) \end{matrix}$	1	$\frac{1}{2}$	1	0	$\frac{1}{2}$	$\frac{2}{3}$	$\frac{1}{6}$
2	u_R^c1	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & [-] & & (+)(+) & & (+)(-) & (-) & (-) \end{matrix}$	1	$-\frac{1}{2}$	1	0	$\frac{1}{2}$	$\frac{2}{3}$	$\frac{1}{6}$
3	d_R^c1	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)(+) & & [-] & [-] & & (+)(-) & (-) & (-) \end{matrix}$	1	$\frac{1}{2}$	1	0	$-\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{6}$
4	d_R^c1	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & [-] & & [-] & [-] & & (+)(-) & (-) & (-) \end{matrix}$	1	$-\frac{1}{2}$	1	0	$-\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{6}$
5	d_L^c1	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & (+) & & (+)(+) & & (+)(-) & (-) & (-) \end{matrix}$	-1	$\frac{1}{2}$	-1	$-\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$
6	d_L^c1	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i) & [-] & & [-] & (+) & & (+)(-) & (-) & (-) \end{matrix}$	-1	$-\frac{1}{2}$	-1	$-\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$
7	u_L^c1	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & (+) & & (+)[-] & & (+)(-) & (-) & (-) \end{matrix}$	-1	$\frac{1}{2}$	-1	$\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$
8	u_L^c1	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i) & [-] & & (+)[-] & & (+)(-) & (-) & (-) \end{matrix}$	-1	$-\frac{1}{2}$	-1	$\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$

$\gamma^0 \gamma^7$ and $\gamma^0 \gamma^8$ transform u_R of the 1st row into u_L of the 7th row, and d_R of the 4rd row into d_L of the 6th row,

doing what the Higgs and γ^0 do in the Stan. model.



In the standard model the families exist by assumption.

In the **spin-charge-family-theory the families are created.**

- γ^a transforms $\binom{ab}{k}$ into $[-k]$, never to $\binom{ab}{k}$.
 S^{ab} transform one family member into another one.
- $\tilde{\gamma}^a$ transforms $\binom{ab}{k}$ into $[k]$, never to $[-k]$.
 \tilde{S}^{ab} transform a family member into the same family member of another family.

Eight families of u_R with the spin 1/2 of a particular colour and of a **colourless** ν_R :

I_R	u_R^{c1}	03 12 56 78 9 10 11 12 13 14 (+i) [+] [+] (+) (+) [-] [-]	ν_R	03 12 56 78 9 10 11 12 13 14 (+i) [+] [+] (+) (+) (+) (+)
II_R	u_R^{c1}	03 12 56 78 9 10 11 12 13 14 [+i] (+) [+] (+) (+) [-] [-]	ν_R	03 12 56 78 9 10 11 12 13 14 [+i] (+) [+] (+) (+) (+) (+)
III_R	u_R^{c1}	03 12 56 78 9 10 11 12 13 14 (+i) [+] (+) [+] (+) [-] [-]	ν_R	03 12 56 78 9 10 11 12 13 14 (+i) [+] (+) [+] (+) (+) (+)
IV_R	u_R^{c1}	03 12 56 78 9 10 11 12 13 14 [+i] (+) (+) [+] (+) [-] [-]	ν_R	03 12 56 78 9 10 11 12 13 14 [+i] (+) (+) [+] (+) (+) (+)
V_R	u_R^{c1}	03 12 56 78 9 10 11 12 13 14 (+i) (+) (+) (+) (+) [-] [-]	ν_R	03 12 56 78 9 10 11 12 13 14 (+i) (+) (+) (+) (+) (+) (+)
VI_R	u_R^{c1}	03 12 56 78 9 10 11 12 13 14 (+i) (+) [+] [+] (+) [-] [-]	ν_R	03 12 56 78 9 10 11 12 13 14 (+i) (+) [+] [+] (+) (+) (+)
VII_R	u_R^{c1}	03 12 56 78 9 10 11 12 13 14 [+i] [+] (+) (+) (+) [-] [-]	ν_R	03 12 56 78 9 10 11 12 13 14 [+i] [+] (+) (+) (+) (+) (+)
$VIII_R$	u_R^{c1}	03 12 56 78 9 10 11 12 13 14 [+i] [+] [+] [+] (+) [-] [-]	ν_R	03 12 56 78 9 10 11 12 13 14 [+i] [+] [+] [+] (+) (+) (+)

Before the break of

$SO(1, 3) \times \mathbf{SU}(2)_I \times \mathbf{SU}(2)_{II} \times \mathbf{U}(1)_{III} \times SU(3)$ into

$SO(1, 3) \times \mathbf{SU}(2)_I \times \mathbf{U}(1)_I \times SU(3)$

all the eight families are massless.



At the symmetry $SO(1,7) \times U(1)_{II} \times SU(3)$ there are $2^{(1+7)/2-1} (= 8)$ massless families of **fermions**

which stay massless also after the break into $SO(1,3) \times SU(2)_I \times SU(2)_{II} \times U(1)_{II} \times SU(3)$.

- The **scalar fields** $\tilde{A}_S^{\tilde{A}i}$ and A_S^{Bj} , in adjoint representations with respect to the family groups, are obviously **doublers** with respect to the weak charge group. The mass term

$$\sum_{s=[7],[8]} \bar{\psi}_L \gamma^s (\mathbf{p}_s - \sum_{\tilde{A},i} \tilde{g}^{\tilde{A}} \tilde{\tau}^{\tilde{A}i} \tilde{A}_S^{\tilde{A}i} - \sum_{B,j} \mathbf{g}^B \tau^{Bj}, \mathbf{A}_S^{Bj}) \psi_R$$

namely does what the *standard model* Higgs does:
 Transforms the right handed quarks and leptons into the left handed partners, generating the mass matrices.

- To the break of symmetries from $SU(2)_I \times SU(2)_{II} \times U(1)_{III}$ to $SU(2)_I \times U(1)_I$ only scalar fields which are triplets with respect to \vec{T}^2 and \vec{N}_R (are assumed to) contribute.

$$\tilde{\mathbf{A}}_S^{2i}, \tilde{\mathbf{A}}_S^{\tilde{N}_R i}$$

- To the break of symmetries from $SU(2)_I \times U(1)_I$ to $U(1)$ both kinds of scalar fields (are assumed to) contribute, those which are triplets with respect to \vec{T}^1 and \vec{N}_L

$$\tilde{\mathbf{A}}_S^{1i}, \tilde{\mathbf{A}}_S^{\tilde{N}_L i}$$

and singlets

$$\mathbf{A}_S^{Y'}, \mathbf{A}_S^{Q'}, \mathbf{A}_S^Q.$$



Before the BREAK II the vielbeins (together with the spin connection fields of S^{ab}) manifest the **massless gauge vector fields** in (1+3)

$$g^4 \tau^4 \mathbf{A}_m^4, \quad g^2 \tau^{2i} \mathbf{A}_m^{2i}, \\ g^1 \tau^{1i} \mathbf{A}_m^{1i}, \quad g^3 \tau^{3i} \mathbf{A}_m^{3i},$$

and the vielbeins together with the spin connection fields of \tilde{S}^{ab} and S^{st} manifest in $d = (1 + 3)$ the **scalar gauge fields** of τ^{Ai} and $\tilde{\tau}^{\tilde{A}i}$

$$g_1^1 \tau^{1i} \mathbf{A}_s^{1i}, \quad g_1^1 \tau^{2i} \mathbf{A}_s^{2i}, \\ \tilde{g}^2 \tilde{\tau}^{2i} \tilde{\mathbf{A}}_s^{2i}, \quad \tilde{g}^1 \tilde{\tau}^{1i} \tilde{\mathbf{A}}_s^{1i}, \\ \tilde{g}^{\tilde{N}_R} \tilde{\mathbf{N}}_R^i \tilde{\mathbf{A}}_s^{\tilde{N}_R i}, \quad \tilde{g}^{\tilde{N}_L} \tilde{\mathbf{N}}_L^i \tilde{\mathbf{A}}_s^{\tilde{N}_L i}.$$

The **spin-charge-family** theory action resembles after the first of the two breaks **the standard model** action before the electroweak break.

There are also many differences, like:

- There are **several scalar fields**, with the family **charges** in the **adjoint representations**, while they all are **doublets** with respect to the **weak charge**.
- There is the operator $\frac{1}{2}(\gamma^7 \mp \gamma^8) = (\pm)^{78}$, which does, in the usual way, the **"dressing" job** of the **Higgs**.
- There are **twice four families** predicted at the low energy regime, **four** of them **forming families** out of which there are the **measured** ones. There is the **dark matter family** as well.

Achievements of the **spin-charge-family-theory** so far concerning:

- **Families:** Two decoupled groups of four families, three of the lowest four observed, the lowest of the upper four are expected to form the dark matter.
- **Scalar fields:** Two decoupled groups of scalar fields: contributing to the mass matrices of the twice four families.
- **Massive vector boson fields:** The $SU(2)_{II}$ and the $SU(2)_I$ (the weak) bosons.

- The fifth family is stable. Its elm **neutral baryons** (neutrinos also contribute) form the **dark matter**.
- **Direct measurements and cosmological evolution limit my fifth family mass** to
 $10 \text{ TeV} < m_{q_5} c^2 < 10^3 \text{ TeV}$.
- The dark matter baryons are opening an interesting new "fifth family nuclear" dynamics.

hep-ph/0711.4681,p.189-194; *Phys. Rev. D* **80**, 083534 (2009);

The lowest four families

The mass matrix of any family member, of any **quark** and any **lepton**, **obeys the same symmetry** – the symmetry required by the **spin-charge-family theory** on the tree level and (almost) proven to be kept in all loop corrections.

We simplify the present study by assuming:

- The mass matrices are Hermitian and real.
- The mixing matrices are real unitary 4×4 matrices.

The effective Lagrange density for spinors is **after the electroweak break** close to what the **standard model** assumes

$$\mathcal{L}_f = \bar{\psi} (\gamma^m p_{0m} - \mathbf{M}) \psi,$$

$$p_{0m} = \mathbf{p}_m - \{ \mathbf{e} \mathbf{Q} \mathbf{A}_m + \mathbf{g}^1 \cos \theta \mathbf{Q}' \mathbf{Z}_m^{Q'} + \frac{\mathbf{g}^1}{\sqrt{2}} (\tau^{1+} \mathbf{W}_m^{1+} + \tau^{1-} \mathbf{W}_m^{1-}) + g^2 \cos \theta_2 Y' A_m^{Y'} \},$$

$$\bar{\psi} \mathbf{M} \psi = \bar{\psi} \gamma^s \mathbf{p}_{0s} \psi$$

$$p_{0s} = p_s - \{ \tilde{g}^{\tilde{N}_L} \tilde{N}_L \tilde{A}_s^{\tilde{N}_L} + \tilde{g}^{\tilde{Q}'} \tilde{Q}' \tilde{A}_s^{\tilde{Q}'} + \frac{\tilde{g}^1}{\sqrt{2}} (\tilde{\tau}^{1+} \tilde{A}_s^{1+} + \tilde{\tau}^{1-} \tilde{A}_s^{1-}) + e Q A_s + g^1 \cos \vartheta_1 Q' Z_s^{Q'} + g^2 \cos \vartheta_2 Y' A_s^{Y'} \}.$$



Mass matrices of **quarks and leptons** have after the electroweak break **after taking into account loop corrections in all orders a very determined symmetry**

$$\mathcal{M}^\alpha = \begin{pmatrix} -a_1 - a & e & d & b \\ e & -a_2 - a & b & d \\ d & b & a_2 - a & e \\ b & d & e & a_1 - a \end{pmatrix}.$$

- We take the diagonal matrix elements \mathcal{M}_d^α , $\alpha = \{u, d, \nu, e\}$ and the mixing matrices $V_{\alpha\beta}$ for the quark pair and the lepton pair from the experimental data, assuming that there is 4×4 mixing matrix which is unitary.

The unitary conditions for the $n \times n$ matrix when applied on the $(n - 1) \times (n - 1)$ submatrix, determine for $n \geq 4$ the $n \times n$ matrix uniquely.

For an orthogonal matrix this is the case for any n .

If assuming that $(n - 1) \times (n - 1)$ submatrix is unitary, we lose $(2n - 1)$ informations, when the free choice of phases are taken into account $(2n - 1)$ goes into $(2n - 3)$.

For an orthogonal matrix we lose in this case $(n - 1)$ informations.

- Taking into account the invariants

$$\sum_{i=1,4} m_i^\alpha, \quad \sum_{i>j=1,4} m_i^\alpha m_j^\alpha, \quad \sum_{i>j>k=1,4} m_i^\alpha m_j^\alpha m_k^\alpha, \\ m_1^\alpha m_2^\alpha m_3^\alpha m_4^\alpha,$$

determined by the masses of the three families and depending on the fourth family mass, we reduce the number of free parameters of each mass matrix from 6 (7) to 3 (4).

- The orthogonal mixing matrix, if known for three families exactly, determines all $6 = 3 + 3$ free parameters of the two family members.

- This would determine in the **spin-charge-family theory** the **masses and the mixing matrices of the four families of quarks and leptons uniquely** in the case, that **i.** $b_1 = b_2$, that **ii.** all the experimental data would be measured accurately and that **iii.** orthogonality and reality of mixing matrices would be a good assumption.
- The measured values within the **experimental accuracy enable** to determine the **intervals** of the **fourth family members masses**.
- **The accurate enough experiments** would **confirm or exclude** the **fourth family**.

We follow the procedure:

- The diagonalizing matrices S^α and S^β , each depending on 3 (for $b_1 = b_2$ otherwise 4) free parameters, are for real and symmetric mass matrices orthogonal. They follow from the procedure

$$M^\alpha = S^\alpha \mathbf{M}_d^\alpha T^{\alpha\dagger}, \quad T^\alpha = S^\alpha F^\alpha S F^\alpha T^\dagger,$$

$$\mathbf{M}_d^\alpha = (m_1^\alpha, m_2^\alpha, m_3^\alpha, m_4^\alpha),$$

in two ways

$$A.: S^\beta = V_{\alpha\beta}^\dagger S^\alpha, \quad B.: S^\alpha = V_{\alpha\beta} S^\beta,$$

$$A.: V_{\alpha\beta}^\dagger S^\alpha \mathbf{M}_d^\beta S^{\alpha\dagger} V_{\alpha\beta} = M^\beta, \quad B.: V_{\alpha\beta} S^\beta \mathbf{M}_d^\alpha S^{\beta\dagger} V_{\alpha\beta}^\dagger = M^\alpha.$$

We use both ways iteratively.

With Gregor Bregar we **treat quarks and leptons in an equivalent way**:

- **Quarks** (very preliminary, intervals are not yet determined):

$$\mathbf{M}_d^u / \text{MeV}/c^2 = (1.24703, 620.141, 172\,000., 650\,000.?)),$$

$$\mathbf{M}_d^d / \text{MeV}/c^2 = (2.92494, 54.793, 2\,899., 700\,000.?)),$$

$$|V_{ud}|_{ij} = \begin{pmatrix} 0.9740 & -0.2243 & -0.0041 & \mathbf{0.0306} \\ 0.2242 & 0.9737 & -0.0409 & \mathbf{-0.0049} \\ 0.0084 & 0.0403 & 0.986 & \mathbf{0.1616} \\ \mathbf{-0.031} & \mathbf{-0.0052} & \mathbf{-0.162} & \mathbf{0.9864} \end{pmatrix}_{ij},$$

$$\mathcal{M}^u = \begin{pmatrix} 101\,630 & -46\,077 & -46\,154 & -94\,733 \\ -46\,077 & 321\,824 & 315\,685 & -46\,154 \\ -46\,154 & 315\,685 & 309\,681 & -46\,077 \\ -94\,733 & -46\,154 & -46\,077 & 98\,4880 \end{pmatrix} \quad \mathcal{M}^d = \begin{pmatrix} 36\,244 & 104\,497 & 104\,484 & -36\,223 \\ 104\,497 & 315\,176 & 315\,198 & -104\,484 \\ 104\,484 & 315\,198 & 315\,235 & -104\,497 \\ -36\,223 & -104\,481 & -104\,497 & 36\,304 \end{pmatrix}$$

- **Leptons** (very preliminary, intervals are not yet determined):

$$\mathbf{M}_d^\nu / \text{MeV}/c^2 = (5 \cdot 10^{-9}?, 1 \cdot 10^{-8}?, 5 \cdot 10^{-8}?, 60? 000,$$

$$\mathbf{M}_d^e / \text{MeV}/c^2 = (0.510998928?, 105.6583715?, 1776.82? 120 000)$$

$$|V_{\nu e}|_{ij} = \begin{pmatrix} 0.9740 & -0.2243 & -0.0041 & \mathbf{0.0306} \\ 0.2242 & 0.9737 & -0.0409 & \mathbf{-0.0049} \\ 0.0084 & 0.0403 & 0.986 & \mathbf{0.1616} \\ \mathbf{-0.031} & \mathbf{-0.0052} & \mathbf{-0.162} & \mathbf{0.9864} \end{pmatrix}_{ij},$$

$$\mathcal{M}^\nu = \begin{pmatrix} 14\,021 & 14\,968 & 14\,968 & -14\,021 \\ 14\,968 & 15\,979 & 15\,979 & -14\,968 \\ 14\,968 & 15\,979 & 15\,979 & -14\,968 \\ -14\,021 & -14\,968 & -14\,968 & 14\,021 \end{pmatrix} \quad \mathcal{M}^e = \begin{pmatrix} 28\,933 & 30\,057 & 29\,762 & -27\,207 \\ 30\,057 & 32\,009 & 31\,958 & -29\,762 \\ 29\,762 & 31\,958 & 32\,009 & -30\,057 \\ -27\,207 & -29\,762 & -30\,057 & 28\,933 \end{pmatrix}$$

Summarizing properties of quarks and leptons following from the **spin-charge-family** theory and **experimental data**:

- We treat **quarks and leptons in equivalent way**. Differences in the properties of quarks and leptons are due to different couplings of family members to the scalars A_S^Q , $A_S^{Q'}$ and $A_S^{Y'}$.
- **The theory predicts**, so far very preliminary, **masses of the fourth family members within some intervals, due to the inaccuracy of the experimental data.**

Scalar fields at the electroweak break

- There are **two triplets and three singlets** with respect to the family quantum numbers. All are **doublets** with respect to the weak charge: $\phi^{Ai} = [\tilde{A}_{\pm}^{\tilde{N}_{Li}}, \tilde{A}_{\pm}^{\tilde{1}i}, A_{\pm}^Q, A_{\pm}^{Q'}, A_{\pm}^{Y'}]$
- The Lagrange density for scalars are so far assumed

$$\begin{aligned} \mathcal{L}_{sb} &= \frac{1}{2} (p_{0m} \phi^{Ai})^\dagger (p_0^m \phi^{Ai}) - V(\phi^{Ai}), \\ V(\phi^{Ai}) &= \sum_{A,i} \left\{ -\frac{1}{2} (m_{Ai})^2 (\phi^{Ai})^2 + \frac{1}{4} \sum_{B,j} \lambda^{Ai Bj} (\phi^{Ai})^2 (\phi^{Bj})^2 \right\}, \\ p_{0m} &= p_m - g^{Ai} \tau^{Ai} A_m^{Ai}. \end{aligned}$$

- The mass eigenstates Φ^β : $\Phi^{Ai} = \sum_\beta C_\beta^{Ai} \Phi^\beta$.

$$V(\Phi^\beta) = \sum_\beta \left\{ -\frac{1}{2} (m_\beta)^2 (\Phi^\beta)^2 + \frac{1}{4} \lambda^\beta (\Phi^\beta)^4 \right\},$$

$$\frac{\partial V}{\partial \Phi^\beta} \Big|_{v_{Ai}} = 0,$$

- The **scalar fields** γ^0 (\mp) $\tau^{Ai} \Phi_{\mp}^{Ai}$ transform the **right handed family members** into the the corresponding **left handed partners**

$$\gamma^0 \begin{pmatrix} - \\ \end{pmatrix} \tau^{Ai} \Phi_{-}^{Ai} \psi_{(u,v)R} \rightarrow \tau^{Ai} \Phi_{-}^{Ai} \psi_{(u,v)L},$$

$$\gamma^0 \begin{pmatrix} + \\ \end{pmatrix} \tau^{Ai} \Phi_{+}^{Ai} \psi_{(d,e)R} \rightarrow \tau^{Ai} \Phi_{+}^{Ai} \psi_{(d,e)L}.$$

$$\psi_{(\mathbf{L},\mathbf{R})}^{\alpha k}, \Psi_{(\mathbf{L},\mathbf{R})}^{\alpha k'}, \quad \alpha = (u_{L,R}, d_{L,R}, \nu_{L,R}, e_{L,R}),$$

massless and massive k^{th} and k'^{th} component of the four vectors,
 k and k' are the **family** quantum numbers:

We have

$$\psi_{(\mathbf{L},\mathbf{R})}^{\alpha} = S^{\alpha} \Psi_{(\mathbf{L},\mathbf{R})}^{\alpha}$$

$$\begin{aligned} \overline{\Psi}^{\alpha} S^{\alpha\dagger} \mathcal{M}^{\alpha} S^{\alpha} \Psi^{\alpha} &= \overline{\Psi}^{\alpha} \text{diag}(m_1^{\alpha}, \dots, m_4^{\alpha}) \Psi^{\alpha}, \\ S^{\alpha\dagger} \mathcal{M}^{\alpha} S^{\alpha} &= \Phi_{\mathbf{f}}^{\alpha}. \end{aligned}$$

The (**Yukawa!!**) couplings of the scalar fields to the α member of the k^{th} family

$$(\Phi_f^\alpha)_{k k'} \Psi^{\alpha k'} = \delta_{k k'} m_{k'}^\alpha \Psi^{\alpha k'}.$$

The superposition of scalar fields in the mass eigenstates basis which couple to fermions

$$\Phi_{fk}^\alpha = \sum_{\beta} D_k^{\alpha\beta} \Phi^\beta.$$

- The **scalar fields** change, when gaining a nonzero vacuum expectation values, properties of the vacuum. At the electroweak BREAK I in the vacuum the new terms appear. In our technique it is

$$\begin{aligned} \begin{matrix} 78 \\ (-) \end{matrix} \ominus_I &: = \begin{matrix} 78 \\ (-) \end{matrix} Ts_{\vec{N}_L} | \begin{matrix} 56 & 78 \\ ([+] & (+) \end{matrix} \rangle Td_{(-)\vec{\tau}^1} || \begin{matrix} 9 & 1011 & 1213 & 14 \\ [+] & [+] & [+] \end{matrix} \rangle, \\ \begin{matrix} 78 \\ (+) \end{matrix} \oplus_I &: = \begin{matrix} 78 \\ (+) \end{matrix} Ts_{\vec{N}_L} | \begin{matrix} 56 & 78 \\ [-] & (-) \end{matrix} \rangle Td_{(+)\vec{\tau}^1} || \begin{matrix} 9 & 1011 & 1213 & 14 \\ [-] & [-] & [-] \end{matrix} \rangle. \end{aligned}$$

Here $Ts_{\vec{N}_L}$ denotes a triplet with respect to the operators \vec{N}_L and a singlet with respect to \vec{N}_L , while $\begin{matrix} 56 & 78 \\ ([+] & (+) \end{matrix} \rangle Td_{(\mp)\vec{\tau}^1}$ are the two triplets with respect to $\vec{\tau}^1$ and doublets with respect to $\vec{\tau}^1$.

■ Due to

$$\begin{aligned} \tau^{1+}\tau^{1-} \begin{pmatrix} 78 \\ + \end{pmatrix} \oplus_I &= \begin{pmatrix} 78 \\ + \end{pmatrix} \oplus_I, & \tau^{1-}\tau^{1+} \begin{pmatrix} 78 \\ - \end{pmatrix} \ominus_I &= \begin{pmatrix} 78 \\ - \end{pmatrix} \ominus_I, \\ Q \begin{pmatrix} 78 \\ + \end{pmatrix} \oplus_I &= 0 = Q \begin{pmatrix} 78 \\ - \end{pmatrix} \ominus_I, \\ Q' \begin{pmatrix} 78 \\ + \end{pmatrix} \oplus_I &= -\frac{1}{2 \cos^2 \theta_1}, & Q' \begin{pmatrix} 78 \\ - \end{pmatrix} \ominus_I &= \frac{1}{2 \cos^2 \theta_1}, \end{aligned}$$

the **vector gauge fields** $A_m^{1\pm} (= W_m^\pm)$ and $A_m^{Q'}$ ($= Z_m$)
 $= \cos \theta_1 A_m^{13} - \sin \theta_1 A_m^Y$ become massive, while $A_m^Q (= \mathbf{A}_m)$
 $= \sin \theta_2 A_m^{13} + \cos \theta_1 A_m^Y$ stays massless, if $\frac{g^1}{g^Y} \tan \theta_1 = 1$.

- Correspondingly the mass term of the **vector gauge bosons** is

$$(p_{0m} \hat{\Phi}_{\mp}^I)^\dagger (p_0^m \hat{\Phi}_{\mp}^I) \rightarrow$$

$$\left(\frac{1}{2}\right)^2 (g^1)^2 v_I^2 \left(\frac{1}{(\cos \theta_1)^2} Z_m^{Q'} Z^{Q' m} + 2 W_m^+ W^{-m} \right),$$

$$\text{Tr}(\Phi_{\mp}^{vI\dagger} \Phi_{\mp}^{vI}) = \frac{v^2}{2}.$$



What questions is the spin-charge-family theory able to answer?

The stated urgent questions the answers to which would help to make the right next step beyond the standard model.

- **Why there exist families at all?** Or rather: What is the **origin of families?**... offering answers
How many families are there? And what are their properties if there are more than the so far observed ones?... offering answers
- **Why family members – quarks and leptons – manifest so different properties if they all start as massless?** ... offering answers

- How is the **origin of the scalar field** (the Higgs) and the **Yukawa couplings connected with the origin of families?** ... offering answers
How many scalar fields determine properties of the so far (and others possibly to be) observed fermions and masses of bosons? ... offering answers
- **Why are all the scalar fields doublets with respect to the weak charge?** What are their **representations with respect to the family quantum numbers?** ... offering answers
- **Where does the dark matter originate?** ... offering answers
- Where do the **charges and correspondingly the so far (and others possibly be) observed gauge fields originate?** ...

What predictions does the spin-charge-family theory offer?

- There are **four** in the low energy regime, rather than **three**, coupled families of **quarks and leptons**. **Careful measurments of the mixing matrices will show this up.**
- **Quarks and leptons** manifest the **same symmetries of mass matrices**.
- The existence of **four families** explains the properties of **neutrinos**.
- The theory **predicts the intervals** for the masses of the fourth families, the more accurate are the measured properties of quarks and leptons, the narrower will be intervals.
- There are **several scalar fields** which will be observed at the LHC.

- The **dark matter** origin in the **fifth family**.
- There are more than so far observed vector gauge fields.
- There is no supersymmetric partners, at least not to the observed ones.

- From $Tr(\Phi_{\mp}^{vl\dagger} \Phi_{\mp}^{vl}) = \frac{v^2}{2}$ we extract from the masses of gauge bosons one information about the vacuum expectation values of the scalar fields, their coupling constants and their masses.
- Mass matrices of quarks and leptons offer additional information about the scalar fields of the *spin-charge-family* theory.
- Measuring charged and neutral currents, decay rates of hadrons, the scalar fields productions in the fermion scattering events and their decay properties provides us with additional informations.

What are not yet solved problems in the spin-charge-family theory?

The spin-charge-family theory offers the **explanation for the assumptions of the standard model** and **several predictions**. Yet there are several **proofs** needed and **calculations to be made**.

- Although I see formally that $SO(4) \times U(1)_{II}$ must break into $SU(2)_I \times U(1)_I$ leading to the **$SU(2)_{II}$ massive vector gauge fields and the massless weak $SU(2)_I$ vector gauge field**, this must be **proven**.
- Although I see that the symmetry is conserved whatever diagram I look at to see whether or not the symmetry of mass matrices on the tree level is conserved in all orders in loop corrections, this is **not yet a proof**.

- Although we have seen that the **loop corrections** of all the contributions **manifest coherence**, this is **not yet a proof** that this coherence really leads to mass matrices, which manifest then the measured properties of quarks and leptons.
- Also the **properties of scalar fields** wait to be **formally derived**.
- Additional numerical evaluation of the mass matrices of the four families of quarks and leptons are needed.
- Carefull study of predictions of the properties of scalar fields, possibly measured at the LHC, are needed.
- And many additional problems to be solved and measurements to be predicted.

Prediction for the LHC

- **LHC will confirm the existence of several scalar fields.**
Yukawa couplings by themselves guarantee that there are several!!
- **LHC will confirm the fourth family.**
- **NO desert in the future measurements.**