

# *Stop and sbottom search using dileptonic $M_{T2}$ variable and boosted top technique at the LHC*

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arXiv:1303.5776 [hep-ph], collaborators : A. Chakraborty, D. Ghosh and D. Sengupta

## Plan of the talk

- Introduction
- Current status and Our Strategy
- Choice of model parameters and Benchmark Points
- Collider analysis and results
- Summary

## Introduction

- Observation of a new particle at the LHC with mass  $m_h \sim 125$  GeV compatible with the SM Higgs.
- This mass value agrees well with prediction of MSSM.
- In MSSM, the large quadratic divergence in  $m_h^2$  due to top quark loop is cancelled by the scalar partner of top quarks (called stop  $\tilde{t}_i$ , with  $i = 1, 2$ ).
- Stop sector plays a crucial role in determining the Higgs mass  $\implies$  the experimental determination of the stop properties is crucial to understand the nature of SUSY protecting the Higgs mass at EW scale.
- So far LHC has not seen any evidence of SUSY particles, only lower bounds have been put on different SUSY particles.
- Limits on gluino ( $\tilde{g}$ ) and squarks ( $\tilde{q}$ ) currently stands at about 1.5 TeV for  $m_{\tilde{g}} \simeq m_{\tilde{q}}$  and about 1.2 TeV for  $m_{\tilde{g}} \ll m_{\tilde{q}}$ .



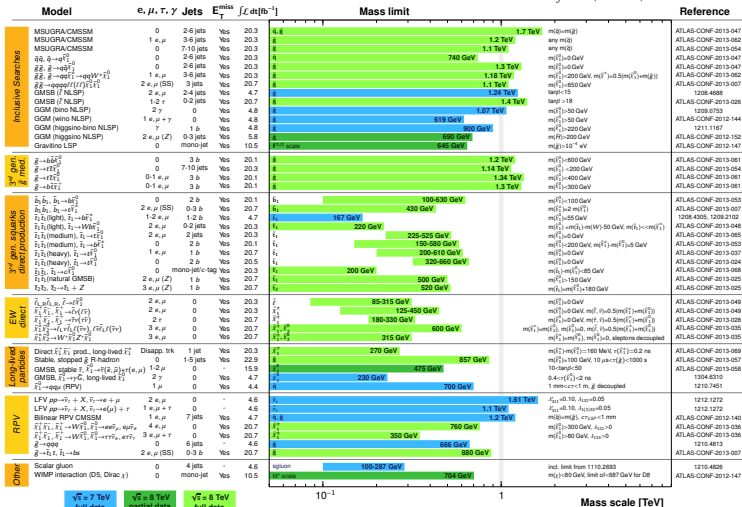
# ATLAS SUSY exclusion

## ATLAS SUSY Searches\* - 95% CL Lower Limits

Status: EPS 2013

ATLAS Preliminary

$$\int \mathcal{L} dt = (4.4 - 22.9) \text{ fb}^{-1} \quad \sqrt{s} = 7, 8 \text{ TeV}$$



\*Only a selection of the available mass limits on new states or phenomena is shown. All limits quoted are observed minus 1 $\sigma$  theoretical signal cross section uncertainty.

## Natural SUSY

- Natural Supersymmetry: superparticles responsible for cancellation of quadratic divergence in Higgs mass are the **third generation squarks**, can be comparatively light to cure the fine-tuning problem of SM.

$$m_h^2 = m_Z^2 \cos^2 2\beta + \frac{3}{4\pi^2} \frac{m_t^4}{v^2} \left( \log \frac{M_S^2}{m_t^2} + \frac{X_t^2}{M_S^2} \left( 1 - \frac{X_t^2}{12M_S^2} \right) \right)$$

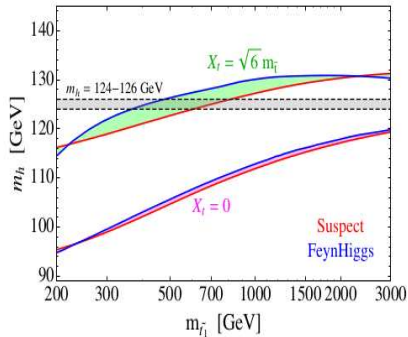
$$M_S^2 = m_{\tilde{t}_1} m_{\tilde{t}_2}$$

$$X_t = A_t - \mu \cot \beta$$

- **Lighter stop/sbottom** : large stop/sbottom tri-linear couplings.
- $m_h \sim 125$  GeV for maximal  $L - R$  mixing  $X_t = \sqrt{6} M_S$

[talk by Carlos Wagner, SUSY 2013]

## MSSM Higgs Mass

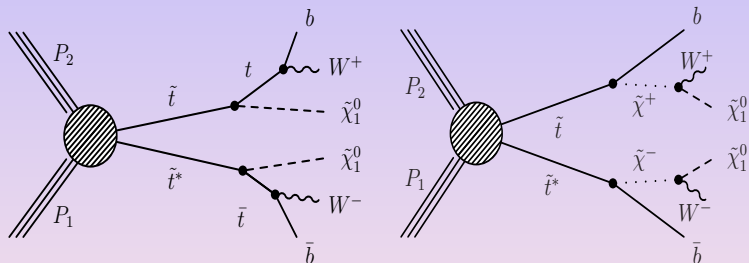


[L.J.Hall et.al, JHEP 04, 131 (2012)]

- Light third generation scenario has an extremely attractive prospect for both the theorists and the experimentalists

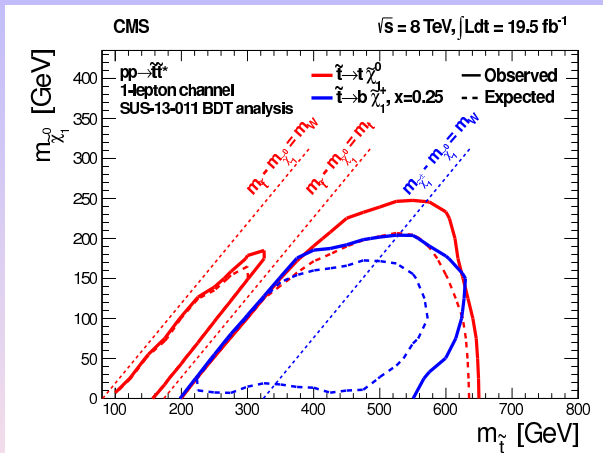
## Stop search @LHC

Di-stop production resulting in  $b\bar{b}W^+W^- + \cancel{E}_T$  in two possible intermediate steps:



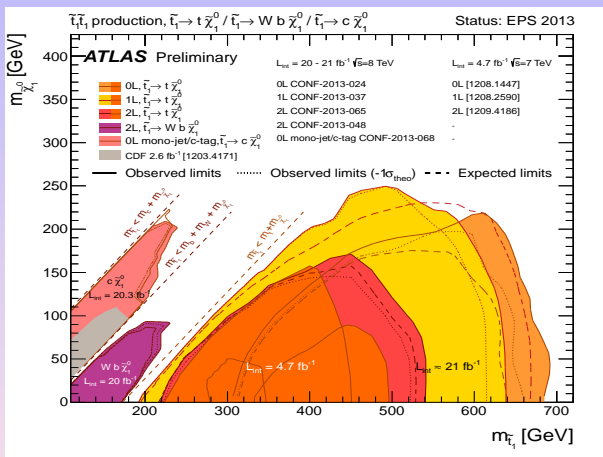


# Stop search @LHC



[see also talk by J. Richman in susy 2013]

# Stop search @LHC

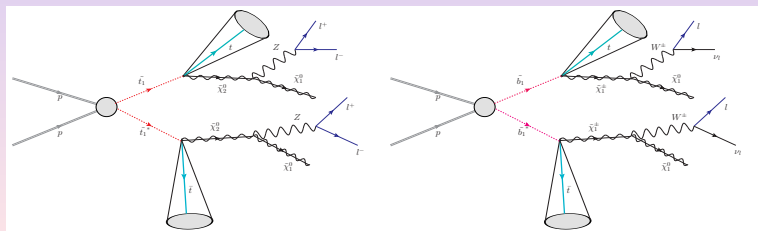


[see also talk by J. Boyd in susy 2013]

## Our Strategy

- Most phenomenological studies assume predominantly right handed stops/sbottom decaying as  $\tilde{t} \rightarrow t\tilde{\chi}_1^0$  and  $\tilde{b}_1 \rightarrow b\tilde{\chi}_1^0$
- Decay of top and bottom squarks to the heavier neutralinos and charginos are quite motivated in natural SUSY spectrum.
- Easy to achieve with lighter stops/sbottoms predominantly left handed.
- We start with Stop and Sbottom pair production having a multi-leptonic final state.

### Typical Process:



## The Signature

- A hadronically decaying top quark, two additional hard leptons and missing transverse momentum (for both stop and sbottom).
- Relatively heavy stop/sbottom, large mass gap  $\tilde{b}_1 - \tilde{\chi}_1^\pm$  and  $\tilde{t}_1 - \tilde{\chi}_2^0$ , sufficiently energetic top quark, apply Jet substructure.
- Two hard leptons with moderately large missing transverse energy, a clean signal.
- A hard cut on  $M_{T2}$ : constructed using the momenta of two hard leptons and missing transverse energy, helps to combat the background.

### NOTE:

- 1 ATLAS and CMS searched for electroweak gauginos,  $pp \rightarrow \tilde{\chi}_1^\pm \tilde{\chi}_2^0 \rightarrow W \tilde{\chi}_1^0 Z \tilde{\chi}_1^0$ , ruled out a range  $\tilde{\chi}_1^\pm = \tilde{\chi}_2^0$  masses as a function of the LSP mass.
- 2 Second neutralino is always assumed to decay exclusively to the LSP and Z boson, limits will not apply directly when second neutralino has non zero branching ratio to the Higgs boson.

## Choice of model parameters

- 1 We vary the left handed third generation mass parameter  $m_{\tilde{Q}_3}$  keeping  $m_{\tilde{t}_R} = m_{\tilde{b}_R} = 2$  TeV.
- 2  $M_3 = 1.5$  TeV while  $M_1$  and  $M_2$  are varied providing various values of  $\tilde{\chi}_i^0$  and  $\tilde{\chi}_i^\pm$
- 3 Higgsino mass parameter  $\mu = 300$  GeV and  $\tan\beta$  is fixed at 10.
- 4  $A_t = -2800$  GeV, keeping other Trilinear coupling set to zero.
- 5  $m_{\tilde{Q}_i} = m_{\tilde{\ell}} = 5$  TeV.
- 6 To generate the particle spectrum we use SuSpect, while decay/branching ratios are calculated using SUSYHIT.

## Benchmark Points

	P1	P2	P3	P4	P5	P6
$m_{\tilde{Q}_3}$	500	500	700	700	900	900
$m_{\tilde{t}_1}$	501.7	501.7	714.2	714.2	918.1	918.1
$m_{\tilde{b}_1}$	525.4	525.4	748.4	748.4	918.1	918.1
$m_{\tilde{\chi}_2^0}$	193.3	193.9	245.9	244.3	297.9	298.6
$m_{\tilde{\chi}_1^\pm}$	192.8	192.8	242.7	242.7	297.0	297.0
$BR(\tilde{b}_1 \rightarrow b \tilde{\chi}_{2,3,4}^0)(\%)$	34.6	34.5	19.3	19.4	19.4	19.4
$BR(\tilde{b}_1 \rightarrow t \tilde{\chi}_{1,2}^\pm)(\%)$	65.4	65.5	80.7	80.6	80.6	80.6
$BR(\tilde{t}_1 \rightarrow t \tilde{\chi}_{2,3,4}^0)(\%)$	34.9	35.2	62.5	62.4	62.5	62.5
$BR(\tilde{t}_1 \rightarrow b \tilde{\chi}_{1,2}^\pm)(\%)$	65.1	64.8	37.5	37.6	37.5	37.5
$BR(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z)(\%)$	33.9	100.0	100.0	22.1	12.8	100.0
$BR(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 h)(\%)$	66.1	0.0	0.0	77.9	87.2	0.0

NOTE: Two scenarios:: Second lightest neutralino dominantly decays via Z boson (benchmarks P2, P3, P6) and/or it decays dominantly via the Higgs (benchmarks P1, P4, P5).

## Signal & Background

$$\begin{aligned}
 pp &\rightarrow \tilde{t}_1 \tilde{t}_1^* \rightarrow t\bar{t}\tilde{\chi}_2^0 \tilde{\chi}_2^0 \rightarrow t\bar{t} + 2Z + 2\tilde{\chi}_1^0 \rightarrow t/\bar{t} + ll + \cancel{p}_T \\
 pp &\rightarrow \tilde{t}_1 \tilde{t}_1^* \rightarrow t\bar{b}\tilde{\chi}_2^0 \tilde{\chi}_1^- \rightarrow t\bar{b} + W^- Z + 2\tilde{\chi}_1^0 \rightarrow t + ll + \cancel{p}_T \\
 pp &\rightarrow \tilde{b}_1 \tilde{b}_1^* \rightarrow t\bar{t}\tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow t\bar{t} + W^+ W^- + 2\tilde{\chi}_1^0 \rightarrow t/\bar{t} + ll + \cancel{p}_T \\
 pp &\rightarrow \tilde{b}_1 \tilde{b}_1^* \rightarrow t\bar{b}\tilde{\chi}_1^- \tilde{\chi}_2^0 \rightarrow t\bar{b} + W^- Z + 2\tilde{\chi}_1^0 \rightarrow t + ll + \cancel{p}_T.
 \end{aligned}$$

- Signal: Two hard leptons associated with atleast a top quark, and missing transverse momentum.
- SM backgrounds:  $t\bar{t} + n \text{ jets}$ ,  $t\bar{t}Z$ ,  $t\bar{t}W$ ,  $tbW$ ,  $t\bar{t}\bar{t}\bar{t}$ ,  $t\bar{t}WW$ .
- We also check,  $tW$  and  $tZ$  events, do not contribute to the background.

## Selection Cuts I

- C1: At least **two isolated leptons (electron and muon)** with the transverse momentum  $p_T^\ell \geq 25$  GeV and the pseudo-rapidity  $|\eta| \leq 3$ .
- C2: Impose  **$M_{T2} > 125$  GeV**

$$M_{T2}(\vec{p}_T^{\ell_1}, \vec{p}_T^{\ell_2}, \vec{p}_T) = \min_{\vec{p}_T = \vec{p}_T^1 + \vec{p}_T^2} \left[ \max\{M_T(\vec{p}_T^{\ell_1}, \vec{p}_T^1), M_T(\vec{p}_T^{\ell_2}, \vec{p}_T^2)\} \right]$$

where  $\ell_1$  and  $\ell_2$  are the two hard leptons and  $M_T(\vec{v}_1, \vec{v}_2)$  is the transverse mass of the  $(\vec{v}_1, \vec{v}_2)$  system which is defined as

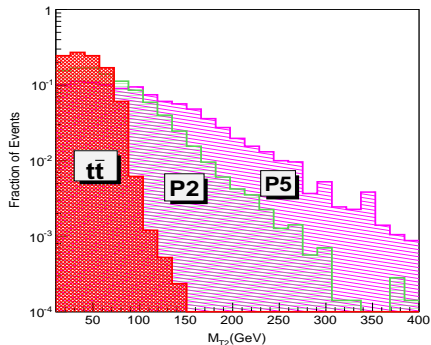
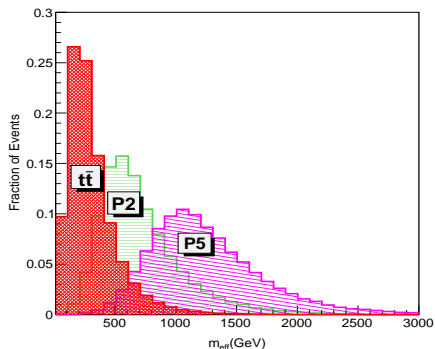
$$M_T(\vec{v}_1, \vec{v}_2) = \sqrt{2|\vec{v}_1||\vec{v}_2|(1 - \cos \phi)},$$

$\phi$  being the (azimuthal) angle between  $\vec{v}_1$  and  $\vec{v}_2$  while  $\vec{p}_T^1$  and  $\vec{p}_T^2$  are a hypothetical split of the total observed missing transverse momentum into two parts.



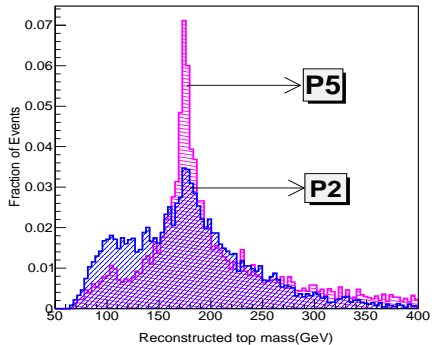
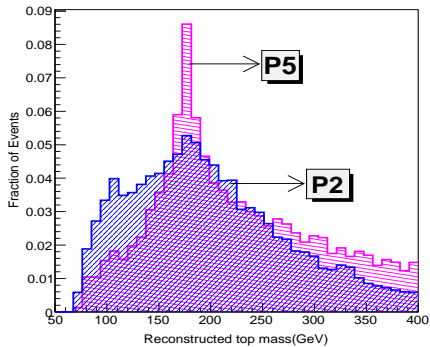
## Selection Cuts II

- C3: Define  $m_{\text{eff}} = \Sigma p_T^j + \Sigma p_T^\ell$ , where the first sum runs over all the hard jets and the second sum is over all the hard and isolated leptons present in an event.  
We choose  $m_{\text{eff}} > 800 \text{ GeV}$ .



## Selection Cuts III

- C4: Our signal final state consists of a number of stable neutralinos and neutrinos, a moderately hard missing transverse momentum cut  $\cancel{p}_T > 150 \text{ GeV}$ .
- C5: **At least one top quark** reconstructing its invariant mass using the jet substructure technique.  
(Johns Hopkins top tagger with the choice of the parameters  $R = 1.5$ ,  $\delta_p = 0.10$  and  $\delta_r = 0.19$  )



## Signal & Background events

Signal	Production Cross-section (fb)	Simulated events (in units of $10^4$ )	No. of events after the cut					$\sigma_S \times 10^2$ (fb)
			C1	C2	C3	C4	C5	
P1	1130	10	10573	821	339	267	55	62.2
P2	1130	10	11091	657	248	205	55	62.2
P3	135	5	8043	1132	712	645	153	41.3
P4	27	5	7713	1207	749	663	153	41.3
P5	27	5	8623	1720	1414	1322	295	15.9
P6	27	5	8543	1679	1343	1281	322	17.4

SM backgrounds	Production Cross-section (fb)	Simulated events (in units of $10^4$ )	No. of events after the cut					$\sigma_B \times 10^2$ (fb)
			C1	C2	C3	C4	C5	
$t\bar{t}$ + jets	918000	4320	1587596	601	39	29	4	8.5
$t\bar{b}W$	61000	600	215807	80	4	2	1	1.0
$t\bar{t}Z$	1121	7	6255	253	52	20	2	3.2
$t\bar{t}W$	769	5	4471	31	3	2	1	1.5
$t\bar{t}W^+W^-$	10	1	1588	33	14	13	6	0.6
$t\bar{t}t\bar{t}$	10	1	1781	31	14	10	4	0.4
Total Background								15.2

## Results

	$m_{\tilde{t}_1}$ (GeV)	Signal( $N_S$ ) ( Background( $N_B$ ))			Significance( $\mathcal{S}$ ) for $\kappa = 10\%$ (30%, 50%)		
		10 fb $^{-1}$	50 fb $^{-1}$	100 fb $^{-1}$	10 fb $^{-1}$	50 fb $^{-1}$	100 fb $^{-1}$
P1	501.6	6.2(1.6)	31.1(8)	62.2(16)	4.9(4.6, 4.1)	10.8(8.4, 6.3)	14.4(9.9, 6.9)
P2	501.6	6.2(1.6)	31.1(8)	62.2(16)	4.9(4.6, 4.1)	10.8(8.4, 6.3)	14.4(9.9, 6.9)
P3	714.2	4.1(1.6)	20.7(8)	41.3(16)	3.2(3.0, 2.7)	7.0(5.6, 4.2)	9.6(6.6, 4.6)
P4	714.2	4.1(1.6)	20.7(8)	41.3(16)	3.2(3.0, 2.7)	7.0(5.6, 4.2)	9.6(6.6, 4.6)
P5	918.1	1.6(1.6)	7.9(8)	15.9(16)	1.3(1.2, 1.1)	2.7(2.1, 1.6)	3.7(2.5, 1.8)
P6	918.1	1.7(1.6)	8.7(8)	17.4(16)	1.3(1.2, 1.1)	2.9(2.3, 1.8)	4.0(2.8, 1.9)

- To take into account the theoretical uncertainty in the estimation of different SM backgrounds, jet energy measurement etc. we calculate significance in the following way :
- Signal significance :  $\mathcal{S} = \frac{N_S}{\sqrt{N_B + (\kappa N_B)^2}}$

## Conclusions

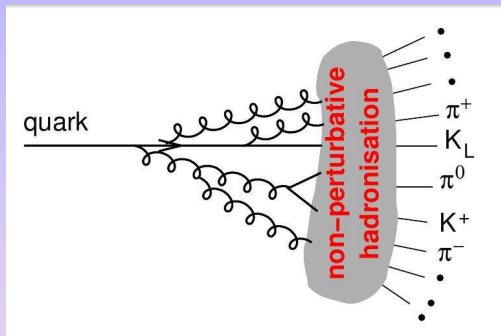
- A Standard Model like Higgs boson of mass  $m_h \simeq 125$  GeV has been discovered at the LHC .
- Current Higgs data  $\implies$  light 3<sup>rd</sup> Generation SUSY particles
- stop and sbottom have been probed up to 650 GeV depending on the decay.
- 14 TeV LHC run will have a rich program to discover the stop and sbottom.
- Signal studied : A top quark with two hard leptons along with substantial missing energy.
- Method used :  $M_{T2}$ ,  $m_{\text{eff}}$  and jet substructure technique to hadronically decaying top quark.
- Outcome : the third generation squarks with masses  $\sim 900$  GeV can be probed at the 14 TeV LHC with a  $100 \text{ fb}^{-1}$  data set.

Thank You!

## Backup Slides



## Jets: Footprints of Partons



### *Jets can serve two purposes:*

They can be **observables**, that one can calculate and measure in an experiment.

They can be **Tools** that one can employ to extract specific properties of the final state.

## Construction of Jets

- The Construction of Jets is ambiguous.

### Why ?

1. Which particles get together into a common Jet?

⇒ There is **NO** Unique way to group hadrons.

⇒ **JET Algorithm**

2. How to combine the particles?

⇒ **Recombination Scheme**

- Most Commonly used: Direct 4-Vector sum ( **E Scheme** )

**Jet Algorithm + Recombination Scheme = Jet Definition**

- Jets Algorithms are broadly of two classes:
  - Cone Algorithms :
  - Sequential Recombination Algorithms

## Jet Algorithms ...Contd

- Sequential Recombination Algorithms

Sequential Recombination Algorithm repeatedly combine closest pair of particles into a single one, according to some distance measurement.

The most general form:

$$d_{ij} = \min(p_{T_i}^{2a}, p_{T_j}^{2a}) \Delta R_{ij}^2 / R^2$$

$$d_{iB} = p_{T_i}^{2a}$$

Where,  $R_{ij}^2 = (\mathbf{y}_i - \mathbf{y}_j)^2 + (\phi_i - \phi_j)^2$

- $a = 1$ :  $k_t$  algorithm
- $a = 0$ : Cambridge/Aachen algorithm
- $a = -1$ : Anti- $k_t$  algorithm
- $y$  : Pseudo-rapidity.
- $\Phi$  : Azimuthal angle

**R** : Sets the minimal interjet separation in the  $y$ - $\phi$  plane

## Sequential algorithm

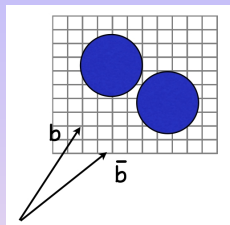
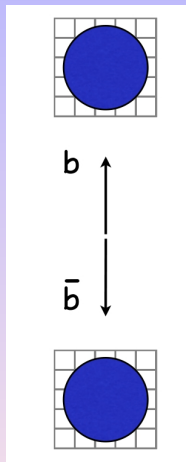
- 1 Start with list of particles
- 2 Calculate distance between all pairs of particles using  $d_{ij}$  and the beam distance for each particles using  $d_{iB}$
- 3 Find the minimum distance in the set  $\{d_{iB}, d_{ij}\}$
- 4 If the minimum is  $d_{ij}$ , recombine  $i$  and  $j$  into a single new particle ( $p_k = p_i + p_j$ ) and return to step 1
- 5 Otherwise, if the minimum is  $d_{iB}$  declare  $i$  to a jet and remove it from the list of particles
- 6 Stop when no particles remain

- Arbitrarily soft particles can form jets  $\implies p_{T\min}^{\text{jets}}$  for hard physics

## Sequential algorithm

- $d_{ij}$  determines the order in which particles are merged in the jet with recombinations that minimizes  $d_{ij}$  first
- $k_t$  algorithm tends to merge low- $p_T$  particles earlier
- CA merges pairs in strict angular order
- Anti- $k_t$  tends to cluster particles with hard  $p_T$  earlier producing jet with less interesting substructure

## No Boost vs Boost

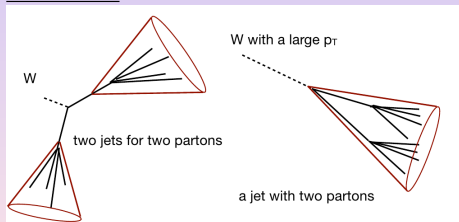


$$m_H = 120 \text{ GeV}, p_T \gtrsim 200 - 300 \text{ GeV} \Rightarrow \text{large boost} \Rightarrow$$
$$\Delta R \approx 2m_H/p_T \approx 1.2 - 0.8$$
$$\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2}$$

$H \rightarrow b\bar{b}$  at rest  $\Rightarrow$  Two back to back jets

## Fat jets

- Quantitatively, consider the following thumb rule for a two-body decay: To resolve the two partons of a  $X \rightarrow q \bar{q}$  decay, choose a radius (or more generally a jet size) of  $R < 2M_X / P_T$
- For  $P_T \gg M_h$   $R \rightarrow$  very small (Overlap of Jet areas !)
- These highly boosted jets are called "Fat Jets"
- Example: Consider a hadronically decaying W Boson..

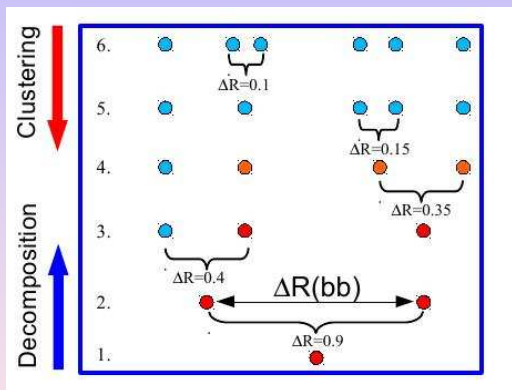


- Question : How do I see the inside of this fat jet ?



## Jet Substructure

The basis of this technique involves an iterative jet clustering algorithm (e.g C/A), examining **subject** kinematics step-by-step, and finally choosing the “**best**” subjects to form the **fat-jet mass**.



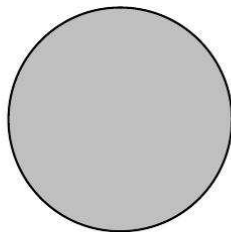
\*\*Ref: Phys. Rev. Lett. 100.242001, Butterworth, Davison, Rubin & Salam

## Jet Decomposition 1

fat jet

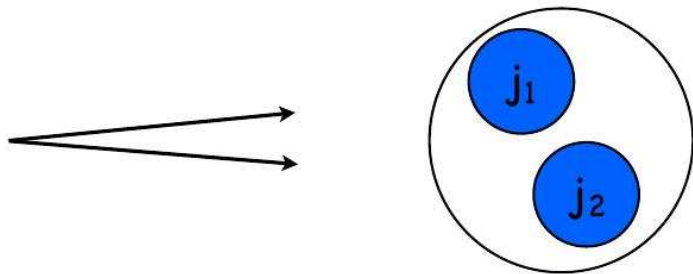


with jet mass:  $m_j$



## Jet Decomposition 2

Step 1: Break the jet  $j$  into two subjets ( $j_1, j_2$ ) by undoing its last stage of clustering s.t  $m_{j_1} > m_{j_2}$ .



## Jet Decomposition 3

Step 2: a) Significant mass drop (MD),

$$m_{j_1} < \mu m_j$$

b) Splitting is nearly Symmetric

$$y = [\min(P_{T_{j_1}}^2, P_{T_{j_2}}^2) / m_j^2] \Delta R_{j_1, j_2}^2 > y_{cut}$$

- Two parameters  $\mu$  and  $y_{cut}$  are independent of Higgs mass and Higgs  $p_t$ .

- $\mu = 0.667$

$$y_{cut} = (0.3)^2$$

⇒ Helps to reject/minimize QCD contamination.

## Jet Decomposition 4

Step 3: If  $y > y_{cut}$ , consider  $j$  as heavy particle neighborhood and exit the loop.

Otherwise

Redefine  $j$  to be  $j_1$  and go back to Step 1.

In practice, above procedure is not optimal for LHC, when the transverse momentum can be around 250-300 GeV.

Since,

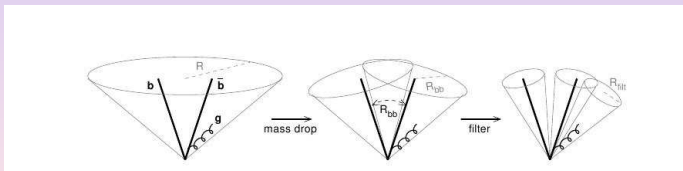
$$m_x \sim 150 \text{ GeV} \quad \Rightarrow \quad R_{j_1, j_2} \sim 1.0 \rightarrow \text{Large}$$

$\Rightarrow$  Significant degradation due the Underlying Events (UE)

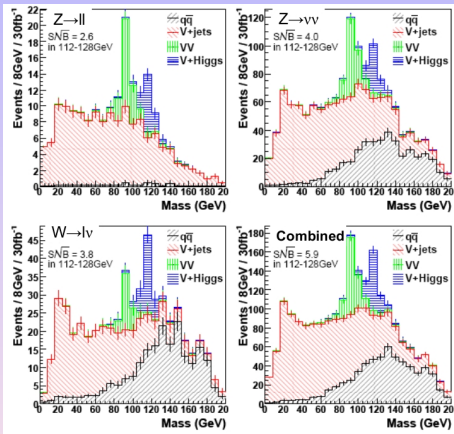
$$\rightarrow \quad \text{UE} \propto R_{j_1, j_2}^4$$

# Filtering

- To minimize UE contamination  $\Rightarrow$  Filter the subjects  $j_1, j_2$  within a finer angular region,  $R_{filt} < R_{j_1, j_2}$
- Consider 3 hardest  $p_T$  subjects 2b & gluon
- Most Effective result ( In the context of Higgs search)  $\Rightarrow$   
 $R_{filt} = \min(R_{j_1, j_2}/2, 0.3)$
- (provided, both the subjects have tagged b's)



# Application : $pp \rightarrow VH, (V = W^\pm, Z)$



- $pp \rightarrow VH$ , with  $V = W^\pm, Z \implies$
- $lvb\bar{b}, llb\bar{b}, \nu\bar{\nu}b\bar{b}$  final state
- For Higgs to be boosted  $p_T(H) > 200$  GeV
- Such a high  $p_T(H) \implies$   
 $\sigma_{\text{boosted}}(WH/ZH) \sim$   
 $5\% \text{ of } \sigma_{\text{tot}}(WH/ZH) @ 14 \text{ TeV}$

- ATLAS simulation @14 TeV with  $30\text{fb}^{-1}$  luminosity :  
 $N_S(m_H \sim 120 \text{ GeV}) \sim 13.5$  and  
 $N_B \sim 20.3 \implies \frac{S}{\sqrt{B}} = 3$

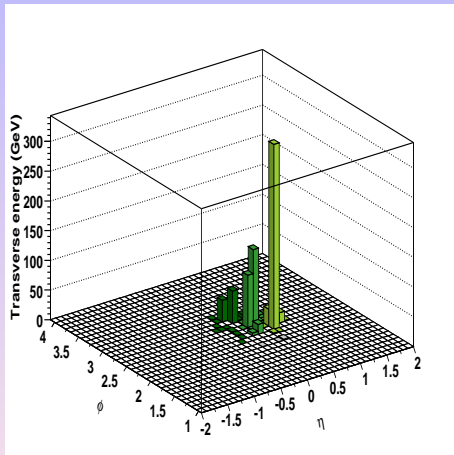
[J.Butterworth *et al.*, PRL (2008)], ATL-PHYS-PUB-2009-088, G. Kribs talk @ Fermilab (2011)

## Top Tagging using Jet Substructure technique

- Particles are clustered into jets of size  $R$  using CA algorithm.
- Each fat jet in the event ( for  $t\bar{t}$  this would be one of the two hardest two ) is declustered, to look into subjets.
- Done by reversing each step in the CA clustering, iteratively separating each jet into two objects.
- Demand  $p_T(i)/p_T(J) > \delta_p$ , else throw away softer jet.
- Continue declustering until one of four things happens:
  - 1 Both objects are harder than  $\delta_p$ .
  - 2 Both objects are softer than  $\delta_p$ .
  - 3 the two objects are too close,  $|\Delta\eta| + |\Delta\phi| < \delta_r$ , where  $\delta_r$  is an additional parameter.
  - 4 or there is only one calorimeter cell left.



# Top Tagging using Jet Substructure technique

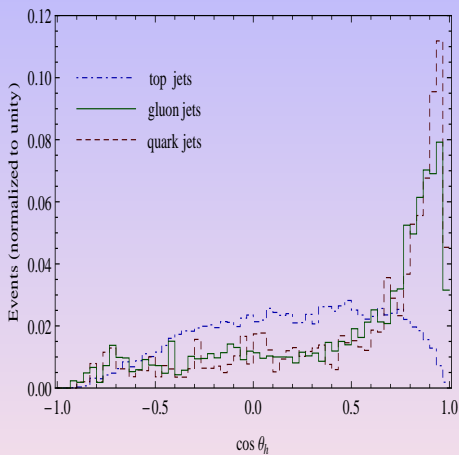


D.E. Kaplan et al. PRL 101, 142001 (2008)

## Top Tagging using Jet Substructure technique

- In case of (1), the two hard objects are considered subjects.
- In cases (2), (3), and (4), the original jet is considered irreducible.
- If an original jet declusters into two subjects, the previous step is repeated on those subjects  $\implies$  2,3,or 4 subjects of the original jet.
- The cases with 3 or 4 subjects are kept, the 4th representing an additional soft gluon emission, while the 2 subjects are rejected.
- Demand :  $M_{3j/4j} \simeq m_t$ .
- Demand :  $M_{2j} \simeq m_W$ .
- Finally we demand that the  $W$  helicity angle satisfy  $\cos \theta_h < 0.7$ .
- For top jets, the distribution is flat,  $W$  decays on-shell, its decay products are isotropically distributed in the  $W$ -rest frame.
- The light quark/ gluon jets distribution diverges as  $1/(1 - \cos \theta_h)$ .

# Top Tagging using Jet Substructure technique



D.E. Kaplan et al. PRL 101, 142001 (2008)