

Stefan Liebler

**Higgs production in the 2HDM
and the MSSM (SusHi)**

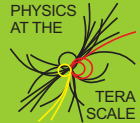
**SUSY 2013
ICTP Trieste, Italy**

27 August 2013

Theoretische Teilchenphysik
Fachbereich C
Bergische Universität Wuppertal

DFG

PHYSICS
AT THE

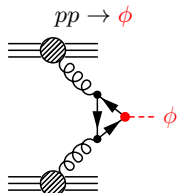


TERA
SCALE

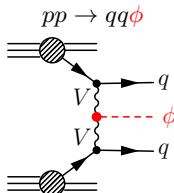
Helmholtz Alliance



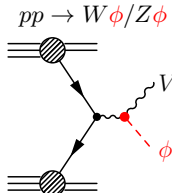
Higgs production processes:



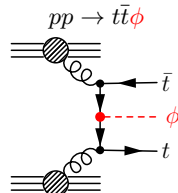
Gluon fusion
Bottom-quark
annihilation



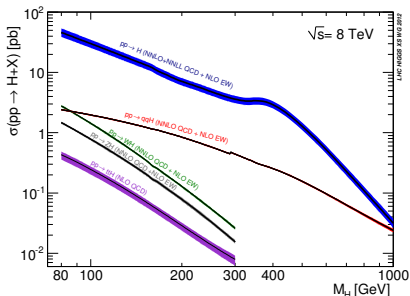
Vector boson fusion



Higgs Strahlung



$t\bar{t}H$ production



This talk: Status of
Higgs production through

- ▷ gluon fusion
- ▷ Higgs Strahlung

in the MSSM and the 2HDM.

Higgs sector of the MSSM:

Two $SU(2)$ doublets $\Phi_u = (\Phi_u^+, \Phi_u^0)^T$ and $\Phi_d = (\Phi_d^0, \Phi_d^-)^T$ mix as follows

$$\begin{array}{c} \text{CP-even Higgs} \quad \text{CP-odd Higgs} \\ \begin{pmatrix} \Phi_u^0 \\ \Phi_d^0 \end{pmatrix} = \begin{pmatrix} v_u \\ v_d \end{pmatrix} + \frac{1}{\sqrt{2}} R_\alpha \begin{pmatrix} h \\ H \end{pmatrix} + \frac{i}{\sqrt{2}} R_\beta \begin{pmatrix} G \\ A \end{pmatrix} \end{array} .$$

8 degrees of freedom result in 5 physical particles: h, H, A, H^\pm .

MSSM Higgs sector input: $\tan \beta = \frac{v_u}{v_d}, m_A^2 \rightarrow m_{h,H}$, Higgs mixing angle α .

Higher orders e.g. by FeynHiggs [Frank Degrassi Hahn Heinemeyer Hollik Rzehak Slavich Weiglein Williams].

Relative strength of Higgs couplings for $\phi = \{h, H, A\}$ (w.r.t. SM couplings)

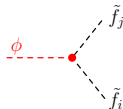
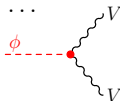
▷ to SM fermions g_f^ϕ : ▷ to gauge bosons g_V^ϕ : ▷ squark couplings $g_{\tilde{f}ij}^\phi$:

$$g_u^h = \frac{\cos \alpha}{\sin \beta}$$

$$g_d^h = -\frac{\sin \alpha}{\cos \beta}$$



$$g_V^h = \sin(\beta - \alpha)$$



Vacuum structure of 2HDMs with Higgs doublets Φ_1 and Φ_2 generally rich.

Assumptions (used in 2HDM analyses by the LHC experiments):

- ▷ CP conservation in the Higgs sector
- ▷ No tree-level FCNCs

4 types of models can be distinguished by Yukawa couplings:

Type	u_R	d_R	e_R
Type I	Φ_2	Φ_2	Φ_2
Type II	Φ_2	Φ_1	Φ_1
Lepton-specific	Φ_2	Φ_2	Φ_1
Flipped	Φ_2	Φ_1	Φ_2

~ MSSM

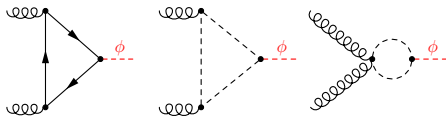
Physical particle content: h, H, A, H^\pm

2HDM input: $m_h, m_H, m_A, m_{H^\pm}, \tan \beta = v_1/v_2, \alpha$ (mixing $h - H$)

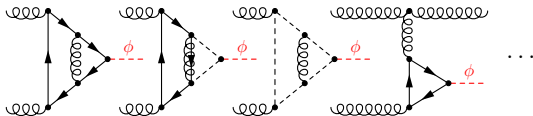
Relative couplings of Higgs fields: $g_f^\phi = F(\alpha, \beta), g_V^\phi$ as before, $g_f^\phi = 0$

[Review of 2HDMs: The Higgs Hunter's guide; Branco Ferreira Lavoura Rebelo Sher Silva; arXiv:1106.0034]

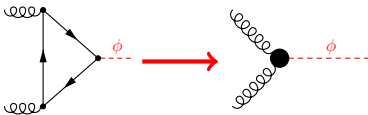
Gluon fusion: \triangleright Leading order (LO) calculation:
quark loops in SM/2HDM (+squark loops in MSSM)



\triangleright Next-to-leading order (NLO) QCD calculation:
includes real contributions



\triangleright Next-to-NLO (NNLO) QCD calculation:
only known in “heavy top-limit” $m_H \ll 2m_t$



σ^{LO}

Correction $\sim 100\%$

σ^{NLO}

Correction $\sim 10\%$

σ^{NNLO}

NLO virtual amplitudes:

- ▷ **gluon-quark**: known analytically (higher orders)

[Spira Djouadi Graudenz Zerwas '95; Harlander Kant '05; . . .]

- ▷ **gluon-squark**: known analytically/numerically

[Anastasiou Beerli Bucherer Daleo Kunszt '06;
Aglietti Bonciani Degrassi Vicini '06; Mühlleitner Spira '06;
Bonciani Degrassi Vicini '07]

- ▷ **gluino-squark-quark** contributions:
semi-analytically known

[Anastasiou Beerli Daleo '08; Mühlleitner Spira Rzehak '10]

Problem with gluino-quark-squark contributions:

Five different masses: $m_q, m_{\tilde{q}_1}, m_{\tilde{q}_2}, m_{\tilde{g}}, p^2 = m_\phi^2$

- ▷ Taylor expansion in small Higgs mass:

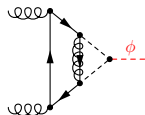
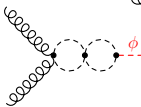
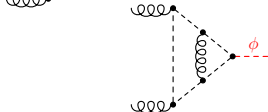
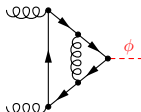
→ top-stop-gluino contribution $m_\phi \ll m_t, m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{g}}$

[Harlander Steinhauser '03 '04 + Hofmann '05; Degrassi Slavich '08]

(NNLO top-stop-gluino contr. [Pak Steinhauser Zerf '10 '12])

- ▷ Expansion in heavy SUSY masses: $m_\phi, m_q \ll m_{\tilde{q}_1}, m_{\tilde{q}_2}, m_{\tilde{g}}$

→ quark-squark-gluino [Harlander Hofmann Mantler '10; Degrassi Slavich '10 + Di Vita '11 '12]



SusHi [Harlander Mantler SL '12] combines efforts achieved in the XS calculation:

(0. Link of SusHi to FeynHiggs or 2HDMC [Eriksson Rathsman Stål '09].)

1. Calculate XS with quark contributions (using resummation) (YR1).
2. Add expanded squark/gluino contributions of third generation (in the MSSM).
3. Add NNLO top effects and electroweak contributions:

$$\sigma(pp \rightarrow \phi + X) = \sigma_{\text{NLO}}^{\text{MSSM}/2\text{HDM}} (1 + \delta_{\text{EW}}^{lq}) + (g_t^\phi)^2 \left(\sigma_{\text{NNLO}}^{t,\text{SM},0} - \sigma_{\text{NLO}}^{t,\text{SM},0} \right)$$

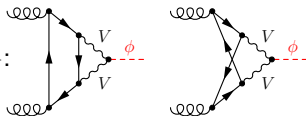
Electroweak contributions by light quarks

ggh@nnlo

(4. Add bottom-quark annihilation and calculate differential quantities.)

Electroweak contributions by light quarks: [Aglietti Bonciani Degrassi Vicini '04 '10]

Relevant diagrams with $V \in \{W, Z\}$:

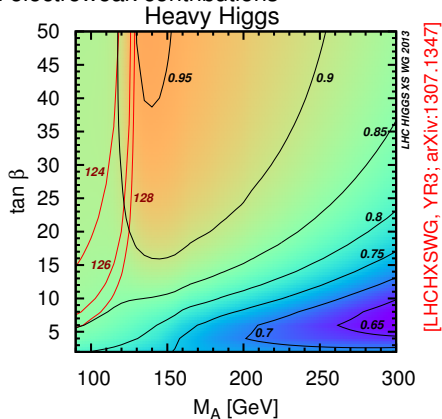
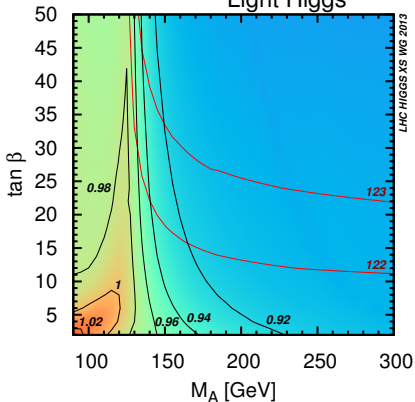


Example from new benchmark scenarios defined by [\[Carena et al.; arXiv:1302.7033\]](#):
“lightstop scenario”

$$m_{\text{SUSY}} = 500\text{GeV}, \quad \mu = 350\text{GeV}, \quad X_t^{\text{OS}} = 2m_{\text{SUSY}} \quad \rightarrow \text{stop masses:}$$

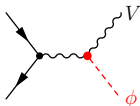
$$A_b = A_t, \quad m_{\tilde{g}} = 1500\text{GeV}, \quad m_{\tilde{l}_3} = 1000\text{GeV} \quad 325\text{GeV and } 670\text{GeV}$$

Ratio $\sigma^{\text{YR3}}/\sigma^{\text{YR1}} \rightarrow$ Effect of squarks and electroweak contributions
Light Higgs

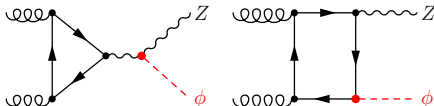


Relevant diagrams for $pp \rightarrow V\phi$ at LO:

Drell-Yan like contributions



Gluon-initiated contributions



$$\sigma_{WH} = \sigma_{WH}^{\text{DY}}(1 + \delta_{WH,EW}),$$

$$\sigma_{ZH} = \sigma_{ZH}^{\text{DY}}(1 + \delta_{ZH,EW}) + \sigma_{gg \rightarrow ZH}$$

Known corrections in the SM:

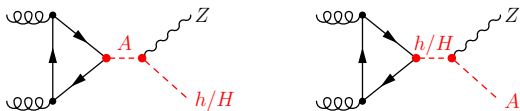
- ▷ σ_{VH}^{DY} calculated up to NNLO with `vh@nnlo` [Brein Djouadi Harlander Zirke '03 '12] with electroweak corrections [Ciccolini Dittmaier Krämer '03]
- ▷ $\sigma_{gg \rightarrow ZH}$ known at NLO [Altenkamp Dittmaier Harlander Rzehak Zirke '12]
- ▷ Top-induced corrections [Brein Harlander Wiesemann Zirke '11]

Procedure in the 2HDM: Reweight σ_{VH} with $(g_V^\phi)^2$?

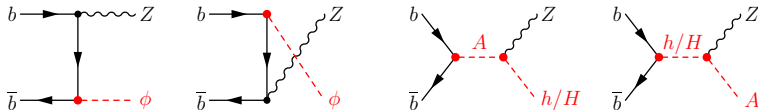
Problem: Gluon-induced contributions are dependent on g_t^ϕ and g_b^ϕ as well!

Higgs Strahlung in the 2HDM: [Harlander SL Zirke '13]

Moreover resonant contributions to $gg \rightarrow Z\phi$:



Even more contributions possible $b\bar{b} \rightarrow Z\phi$:

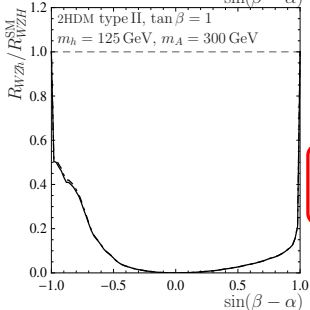
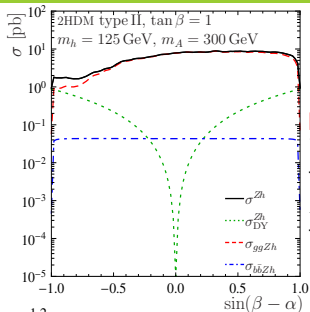
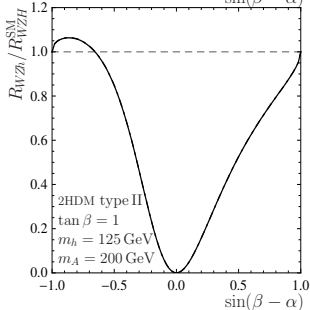
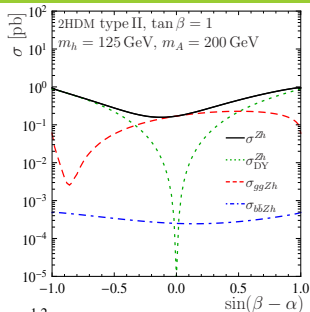


→ $pp \rightarrow Z\phi$ affected by various contributions.

$pp \rightarrow W\phi$ reweighted by $(g_V^\phi)^2$.

→ New physics effects in the ratio $R_{WZ\phi} = \sigma_{W\phi}/\sigma_{Z\phi}$!
Independent of ϕ decay mode, uncertainties reduced.

Implementation in `vh@nnlo` with link to 2HDMC.



Example in the 2HDM:

[Harlander SL Zirke '13]

Vh production

for $\sqrt{s} = 14 \text{ TeV}$

$R_{WZH}^{\text{SM}} = 1.570$

for $m_H = 125 \text{ GeV}$

Check the ratio:

$$R_{WZ\phi} = \sigma_{W\phi} / \sigma_{Z\phi}$$

We showed progress in the calculation of Higgs production for a neutral Higgs ϕ in the SM/MSSM/2HDM.

In case of gluon fusion/bottom-quark annihilation:

- ▷ calculation of MSSM/2HDM gluon fusion XS @NLO including all SUSY, NNLO top and electroweak contributions.
- ▷ calculation of MSSM/2HDM weighted bottom-quark annihilation XS.

→ SusHi

In case of Higgs Strahlung in the 2HDM calculation of all relevant contributions at least at LO \leftrightarrow **Ratio** $\sigma_{W\phi}/\sigma_{Z\phi}$.

→ vh@nnlo (2HDM version published soon.)

Many thanks for your attention!

Where can I get SusHi/vh@nnlo? <http://sushi.hepforge.org> and <http://nnlo.de>



- SusHi
- Changelog
- Manual
- Examples
- Contact
- Download



How can the Higgs sector in a local $SU(2) \times U(1)$ gauge theory be extended?

Measurement of $\rho \sim 1.0004$ [PDG]

Introduce n scalar multiplets ϕ_i with:

- ▷ weak Isospin T_i
- ▷ weak hypercharge Y_i
- ▷ VEVs v_i of neutral comp.

$$\rho = \frac{\sum_{i=1}^n [T_i(T_i + 1) - Y_i^2] v_i}{\sum_{i=1}^n 2Y_i^2 v_i}$$

→ Simplest version: Add multiplets with $T(T + 1) = 3Y^2$
e.g. $SU(2)$ **singlets** with $Y = 0$, $SU(2)$ **doublets** with $Y = \pm \frac{1}{2}, \dots$

Within this talk:

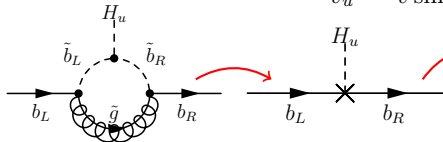
- ▷ Standard Model: One $SU(2)$ doublet
- ▷ Minimal Supersymmetric Standard Model (MSSM): Two $SU(2)$ doublets
- ▷ 2 Higgs Doublet Model (2HDM): Two $SU(2)$ doublets

Resummation of large $\tan \beta$ -enhanced terms in the MSSM

$$\mathcal{L} \supset -Y_t H_u Q t_R + Y_b H_d Q b_R$$

Using $\langle H_u \rangle = v_u$, $\langle H_d \rangle = v_d$ and $v_d^2 + v_u^2 = v^2$, $\tan \beta = v_u/v_d$ we define

$$Y_t = \frac{m_t}{v_u} = \frac{m_t}{v \sin \beta}, \quad Y_b = \frac{m_b}{v_d} = \frac{m_b}{v \cos \beta}$$



$$\mathcal{L}^{\text{eff}} \supset Y_b H_d Q b_R - \tilde{Y}_b H_u^* Q b_R$$

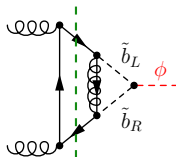
$$\Delta_b = \frac{\tilde{Y}_b v_u}{Y_b v_d} =: \epsilon \tan \beta$$

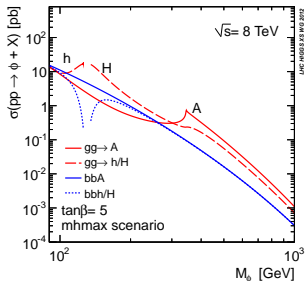
The effective Lagrangian motivates:

$$m_b = Y_b v_d + \tilde{Y}_b v_u = Y_b v_d (1 + \epsilon \tan \beta)$$

$$\Rightarrow Y_b = \frac{m_b}{v_d (1 + \Delta_b)}$$

This replacement implies a resummation of large $\tan \beta$ -enhanced terms:





Enhancement of g_b^ϕ for large $\tan \beta$ in MSSM

Idea: Use results from 5FS and reweight accordingly with resummed MSSM couplings

[Guasch Häfliger Spira '03]:

$$g_b^A = g_b^A \frac{1}{1 + \Delta_b} \left(1 - \frac{1}{\tan^2 \beta} \Delta_b \right)$$

$$g_b^h = g_b^h \frac{1}{1 + \Delta_b} \left(1 - \frac{1}{\tan \beta \tan \alpha} \Delta_b \right)$$

$$g_b^H = g_b^H \frac{1}{1 + \Delta_b} \left(1 + \frac{\tan \alpha}{\tan \beta} \Delta_b \right)$$

$$\left. \begin{aligned} \Delta_{Ab} &= -\frac{C_F}{2\pi} \alpha_s(\mu_r) m_{\tilde{g}} A_b I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, m_{\tilde{g}}^2) \\ \Delta_b &= \frac{C_F}{2\pi} \alpha_s(\mu_r) m_{\tilde{g}} \mu \tan \beta I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, m_{\tilde{g}}^2) \end{aligned} \right\} \Delta_b \rightarrow \Delta_b \frac{1}{1 + \Delta_{Ab}}$$

Specify model, collider,
 \sqrt{s} , Higgs, processes

Give SM input values

MSSM/2HDM input values:

Link `SuSHi` to

▷ FEYNHIGGS

▷ 2HDMC

[Eriksson et al, arXiv: 0902.0851]

Specify PDF sets

Specify VEGAS input

```
Block SUSHI
  1 1 # model: 0 = SM, 1 = MSSM, 2 = 2HDM
  2 0 # 0 = scalar (h), 1 = pseudoscalar (A), 2 = scalar (H)
  3 0 # collider: 0 = p-p, 1 = p-pbar
  4 8000.d0 # center-of-mass energy in GeV
  5 2 # order ggh: -1 = off, 0 = LO, 1 = NLO, 2 = NNLO
      # 3 = ~NNLO stop
  6 2 # order bbh: -1 = off, 0 = LO, 1 = NLO, 2 = NNLO
  7 1 # electroweak cont. for ggh:
      # 0 = no, 1 = light quarks at NLO, 2 = SM EW factor

Block SMINPUTS # Standard Model inputs
  1 1.27934000e+02 # alpha_em^(-1)(MZ) SM MSbar
  ....

Block MINPAR # SUSY breaking input parameters
  3 1.00000000e+01 # tanb

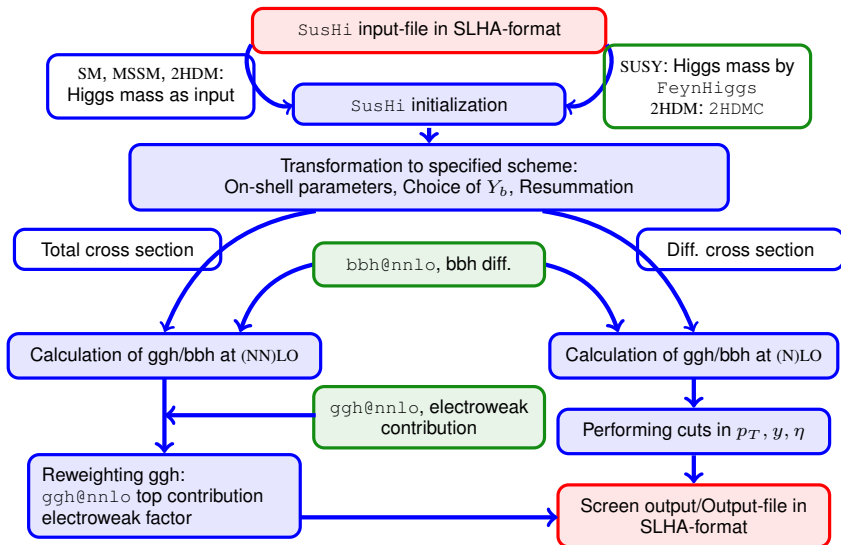
Block EXTPAR
  3 800.d0 # M_3
  11 2000.d0 # A_t
  ....

Block ALPHA
  -8.3691204e-01 # mixing in Higgs sector

Block MASS
  25 120.76695d0 # Higgs mass h
  ....
  ....

Block PDFSPEC
  1 MSTW2008lo68cl.LHgrid # name of pdf (lo)
  2 MSTW2008nlo68cl.LHgrid # name of pdf (nlo)
  3 MSTW2008nnlo_asmzrange.LHgrid # name of pdf (nnlo)
  4 0 # set number

Block VEGAS
  1 10000 # number of points
  2 5 # number of iterations
  3 10 # print: 0 = no output, 1 = prettyprint, 10 = table
```



Example output file

```
# Please cite the following papers (for this run):
# Harlander:2012pb
.....
# Heinemeyer:1998np
# Degrassi:2002 fi
# Frank:2006yh
Block SUSHlgh # Bon appetit
      1      1.59566551E+01 # ggh XS in pb
Block SUSHlbbh # Bon appetit
      1      2.67975811E-01 # bbh XS in pb
Block XSGGH # ggh MSSM-Cross sec. in pb (w/o EW)
      2      1.13849524E+01 # NLO
      21     1.14675980E+01 # NLO gg
      22     -1.02733041E-01 # NLO qg
      23     2.00874475E-02 # NLO qq
Block XSGGHEFF # ggh MSSM-Cross sec.
      1      1.49056433E+01 # ggh@NLO MSSM
      2      1.88154287E+01 # ggh@NNLO MSSM
      3      5.81396602E-02 # electroweak factor
Block XSBH # bbh MSSM-Cross sec. in pb
      1      3.72508379E-01 # LO
      2      3.35738356E-01 # NLO
      3      2.67975811E-01 # NNLO
.....
Block MASSOUT
      5      4.21300000E+00 # m_b(m_b), MSbar
      6      1.73200000E+02 # m_t(pole)
      23     9.11876000E+01 # m_Z
      24     8.03980311E+01 # m_W
      25     1.23484421E+02 # MSSM-Mh in GeV
1000005   4.93350465E+02 # sbottom1 mass in GeV
2000005   5.18897088E+02 # sbottom2 mass in GeV
1000006   3.23616710E+02 # stop1 mass in GeV
2000006   6.71663496E+02 # stop2 mass in GeV
```

SusHi usage: Current ATLAS 2HDM analysis $\phi \rightarrow WW \rightarrow l\nu l\nu$

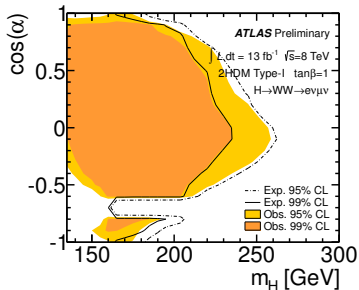
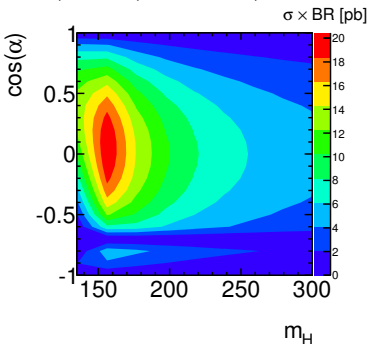
- ▶ Gluon fusion: σ from SusHi
- ▶ Vector boson fusion: $\sigma^{\text{VBF}} = \sigma^{\text{VBF,SM}}(g_V^\phi)^2$
- ▶ Decays:

$$\text{BR}(\phi \rightarrow WW) = \frac{\Gamma(H \rightarrow WW)(g_W^\phi)^2}{\Gamma(H \rightarrow WW)(g_W^\phi)^2 + \Gamma(H \rightarrow b\bar{b})(g_b^\phi)^2}$$

2HDM type I with $\tan\beta = 1$ and light Higgs at $m_h = 125$ GeV

$\sigma(gg \rightarrow H) \times \text{BR}(H \rightarrow WW)$

Exclusion plot for heavy Higgs



[courtesy of ATLAS, ATLAS-CONF-2013-027]